

# Algorithmic Improvisation for Dependable and Secure Autonomy

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Joint work with:

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Ilge Akkaya, Alexandre Donze, Rafael Valle, Edward A. Lee,  
Alberto Sangiovanni-Vincentelli, David Wessel



Microsoft Research India

August 1, 2019

*Vet-iCal*





# Human Cyber-Physical Systems (h-CPS)



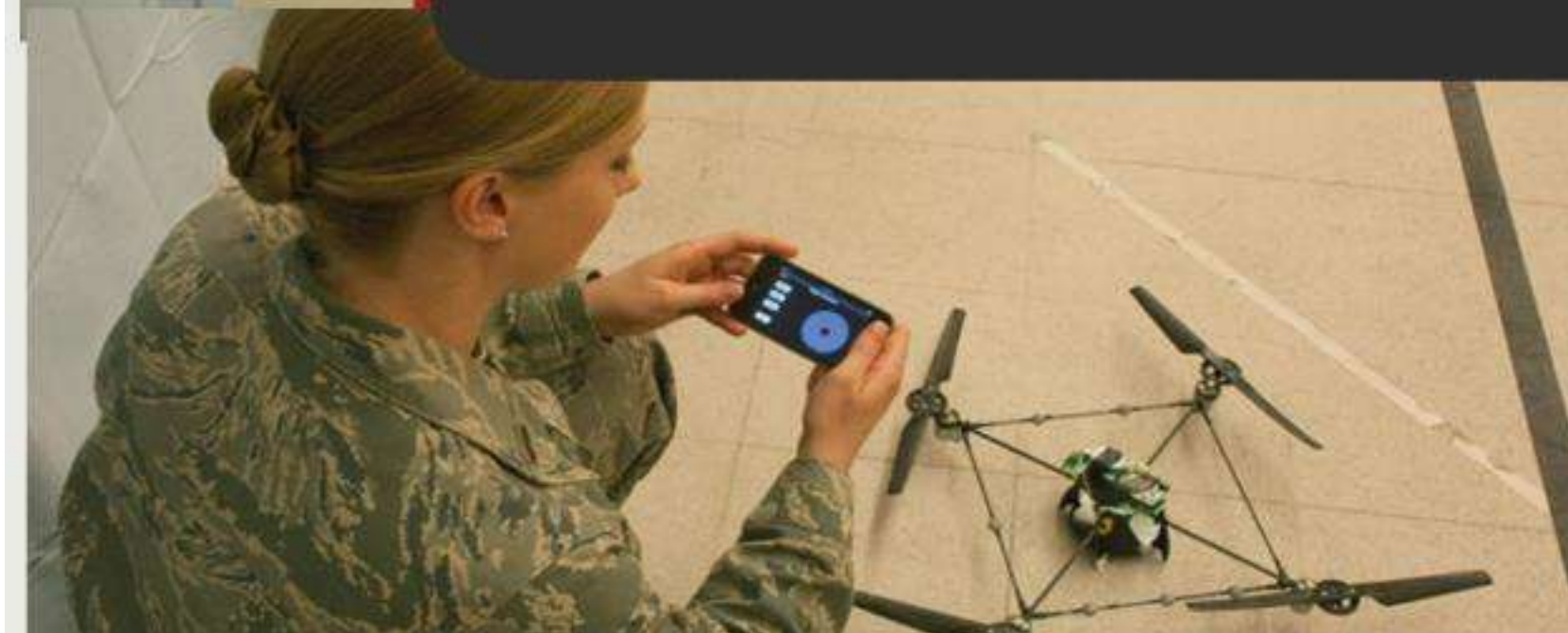




## Human Cyber-Physical Systems (h-CPS)



**“Safety critical”** systems *interacting* with humans, often in a complex environment











DRIVERLESS CAR SAFETY—

# Report: Software bug led to death in Uber's self-driving crash

Sensors detected Elaine Herzberg, but software reportedly decided to ignore her.

TIMOTHY B. LEE - 5/7/2018, 3:12 PM

[NTSB]





Investigators with the federal agency determined that the car's detection systems, including radar and laser instruments, observed a woman walking her bicycle across the road roughly six seconds before impact — likely enough time, in other words, for a vehicle driving 43 mph to brake and avoid fatally injuring the woman.

But it did not immediately identify the woman as a human pedestrian. Instead, the agency said, "as the vehicle and pedestrian paths converged, the self-driving system software classified the pedestrian as an unknown object, as a vehicle, and then as a bicycle with varying expectations of future travel path."

ars TECHNICA

BIZ

DRIVERLESS CAR SAFETY—

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# A Formal Methods Approach

*Formal Methods*: rigorous algorithmic techniques to model, design, and analyze systems based on formal mathematical reasoning.

“Towards Verified Artificial Intelligence”, S. A. Seshia et al., 2016:  
<https://arxiv.org/abs/1606.08514>

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**Prove** rigorous guarantees when possible;

do ***formally-guided, intelligent simulation/testing*** when not.

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# Message of this Talk



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*Randomness* can play a crucial role in  
Formal Methods for Autonomy!



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- Verification – Constrained-Random Simulation, Probabilistic Verification



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- Modeling Autonomous Systems and Their Environments
- Verification – Constrained-Random Simulation, Probabilistic Verification
- Synthesis: Randomized Planning/Control



# Randomized Formal Methods for Safe Autonomy



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Randomized  
Controller Synthesis  
(CAV'18)



Diverse, unbiased  
but safe trajectories



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Realistic models of  
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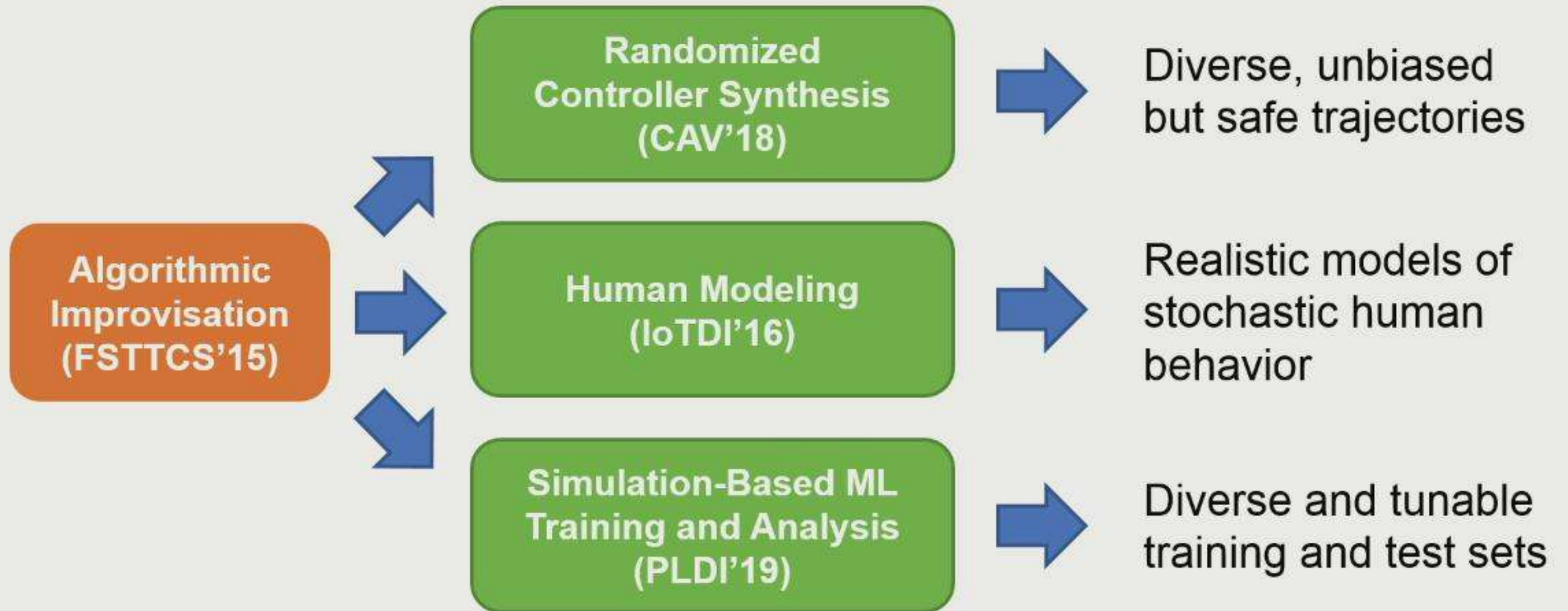
**Simulation-Based ML  
Training and Analysis  
(PLDI'19)**



Diverse and tunable  
training and test sets



# Randomized Formal Methods for Safe Autonomy





# Why Randomness: Variety/Coverage

- Train/test set generator for an object-detecting neural network
  - “Generate images of bumper-to-bumper traffic”
  - Huge and diverse space of possibilities – randomness lets you cover it well

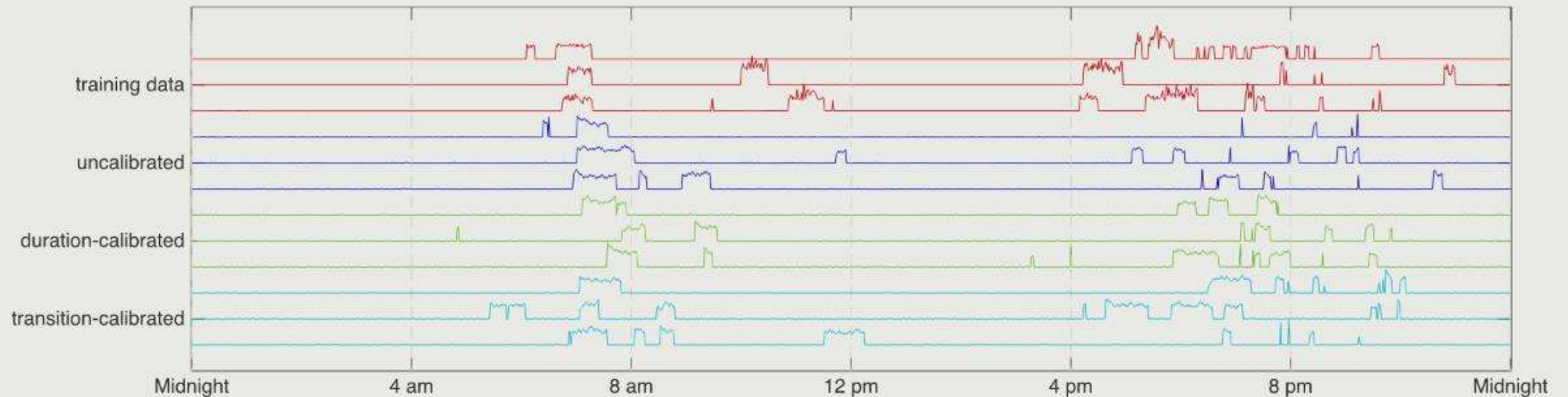


Fremont et al., *Scenic: A Language for Scenario Specification and Scene Generation*, PLDI 2019 (to appear).



# Why Randomness: Realism

- Home automation lighting controller
  - “Mimic the user’s typical behavior while they are away”
  - Deterministic models unrealistic – human behavior is random

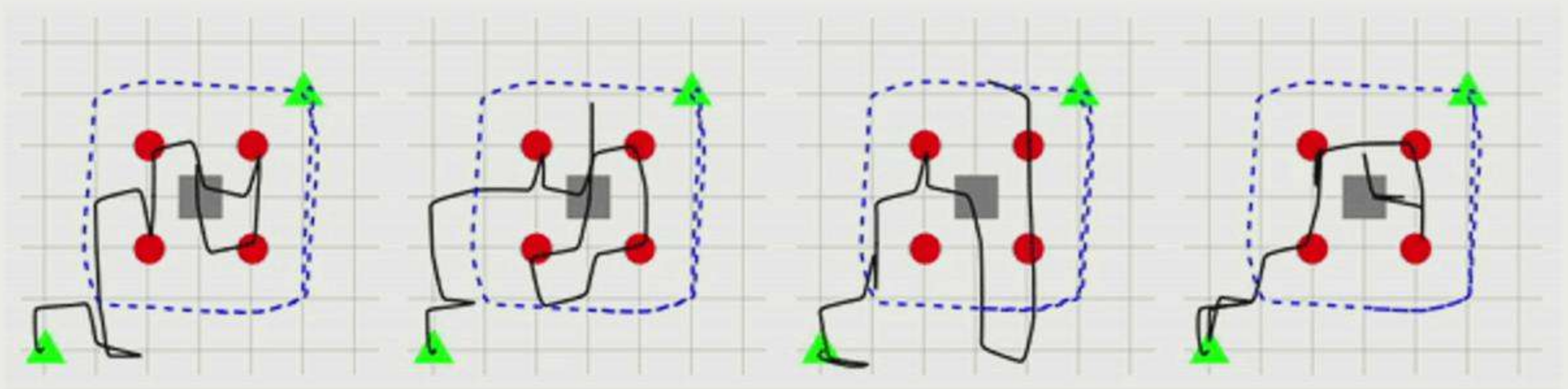


Akkaya et al., *Control Improvisation with Probabilistic Temporal Specifications*, IoTDI 2016.



# Why Randomness: Unpredictability

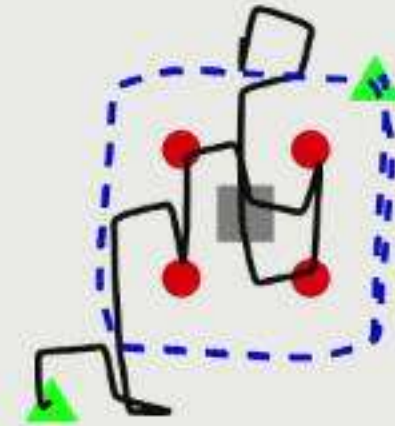
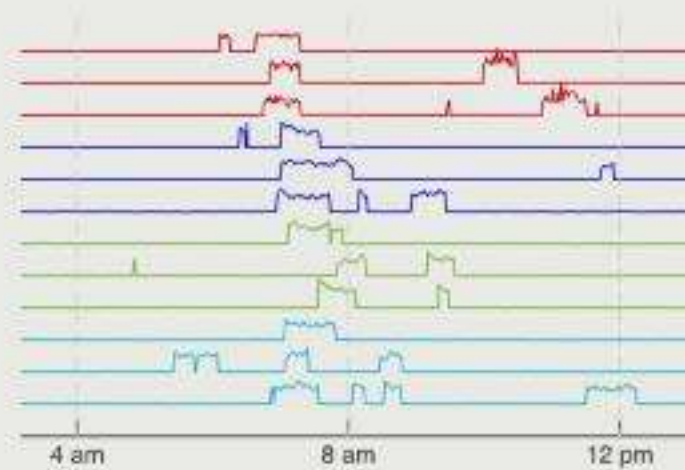
- Surveillance robot
  - “Patrol an area, visiting each important location sufficiently often”
  - Using a random route makes the robot’s future location harder to predict



Fremont and Seshia, *Reactive Control Improvisation*, CAV 2018.

# Randomness with Guarantees

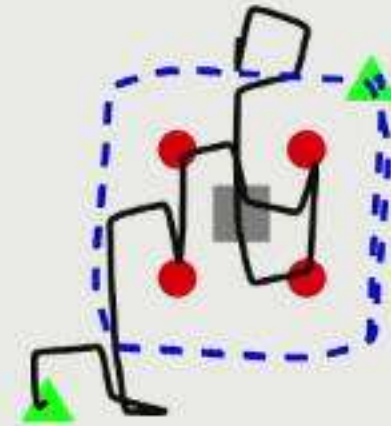
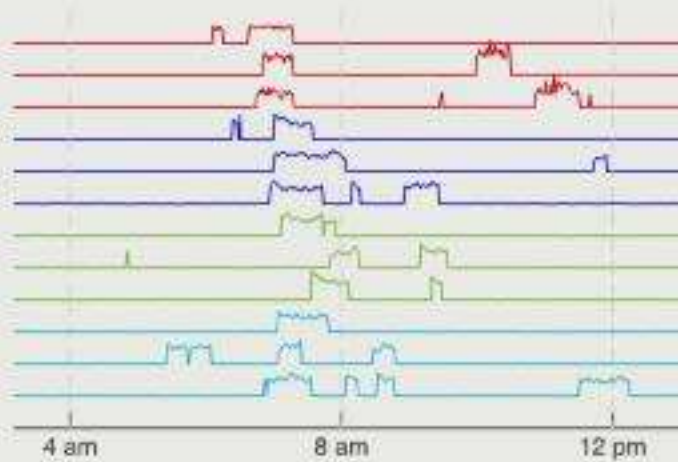
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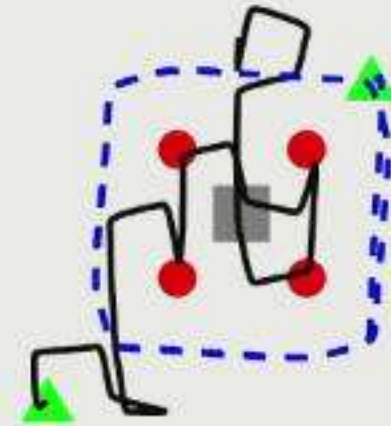
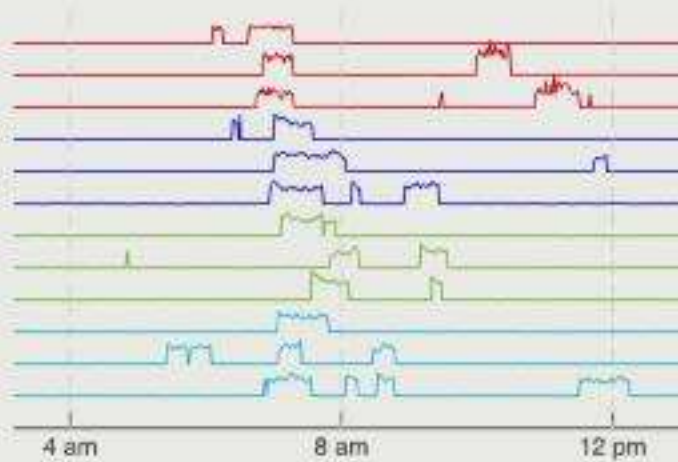
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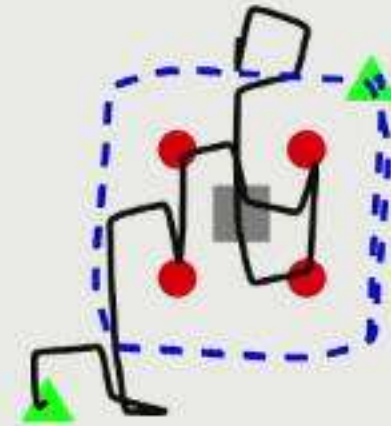
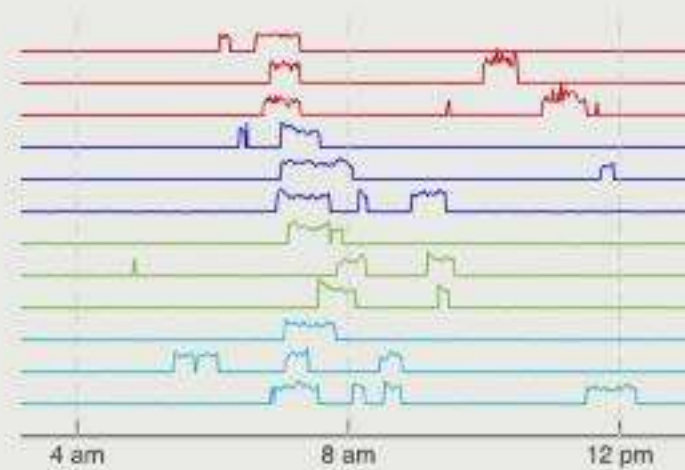
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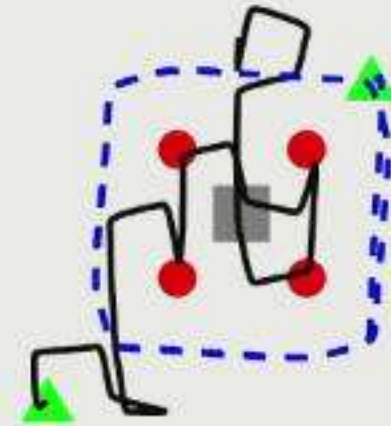
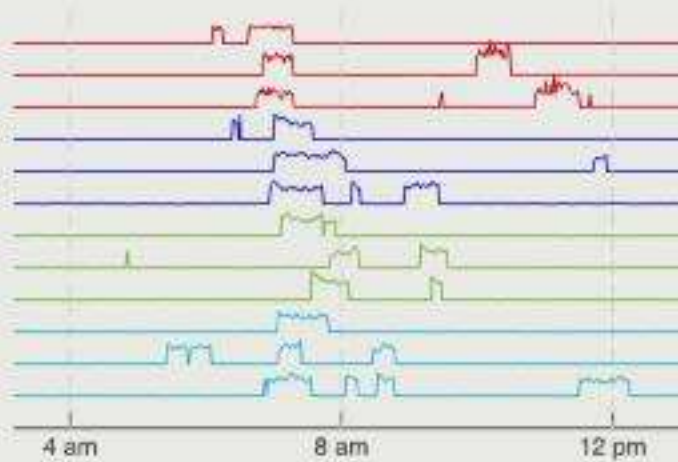
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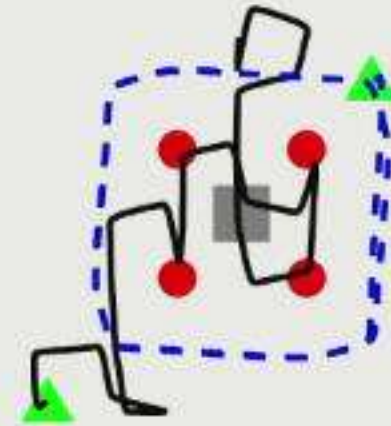
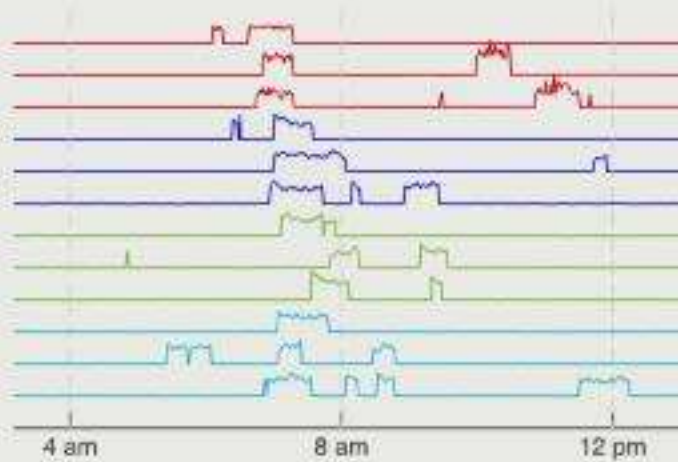
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- ***How to design a system with random but controlled behavior?***

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- A framework for automatically synthesizing (reactive) systems with random behavior but formal guarantees:
  - Guaranteed safety (hard and soft constraints)
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- **Key novelty: Randomness is *part* of the specification!**

# Outline

1. Control Improvisation
  - Definition and motivating applications



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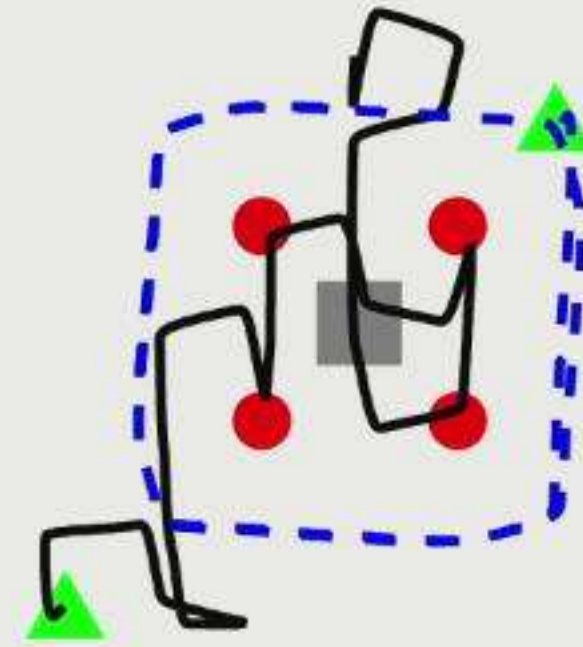
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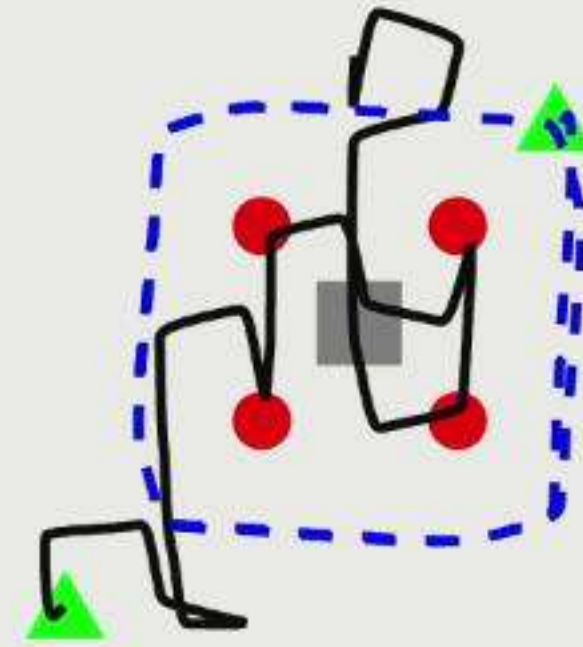
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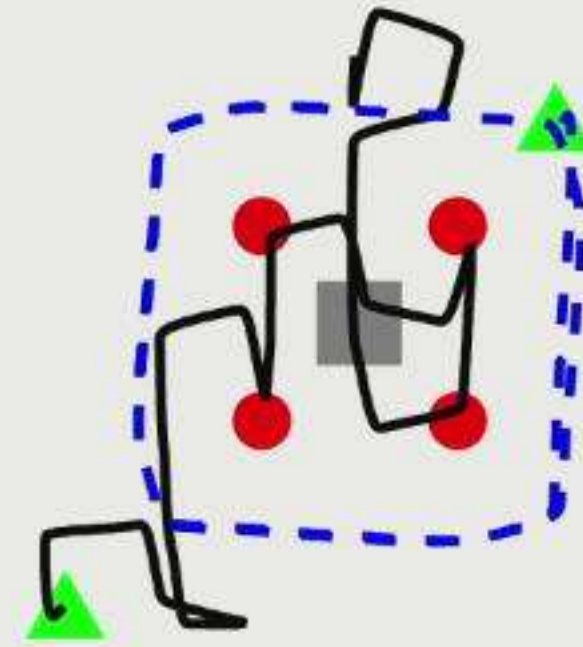
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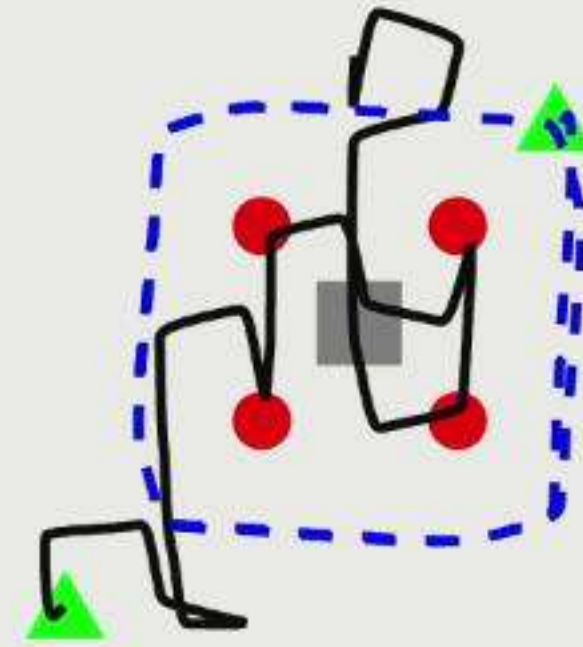
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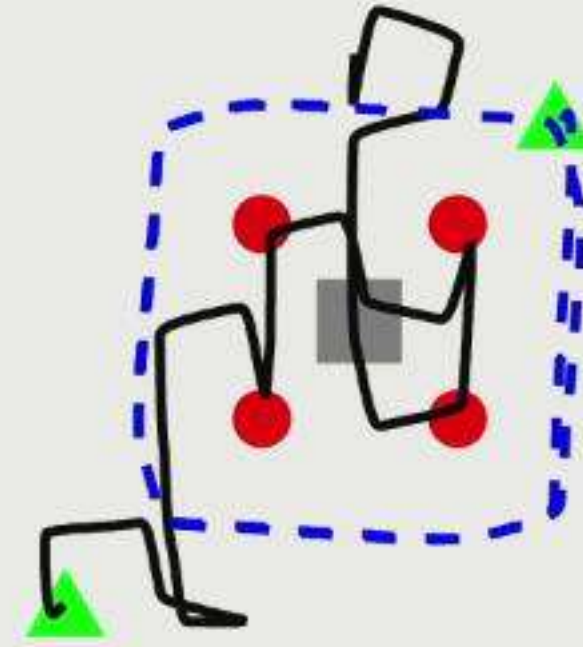
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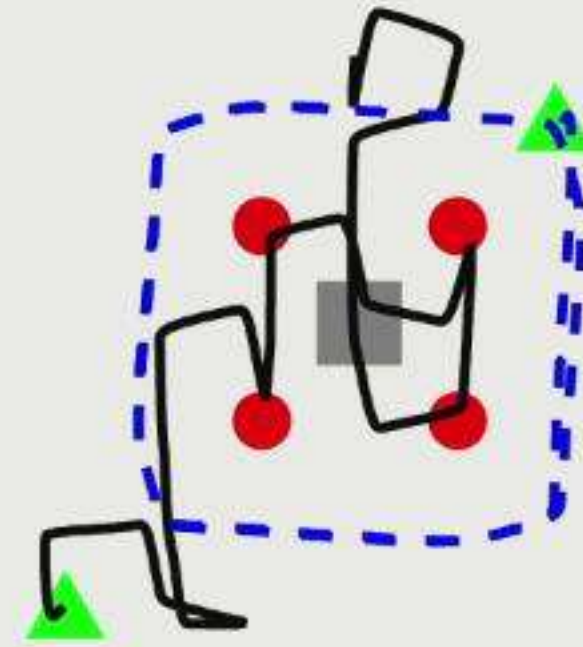
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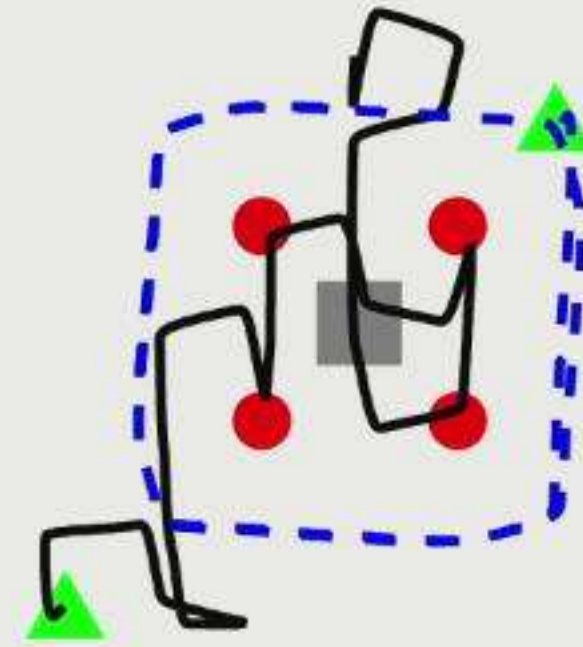
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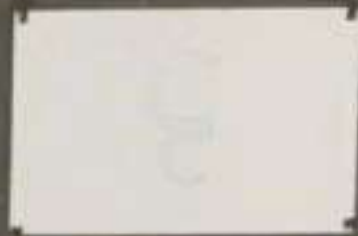
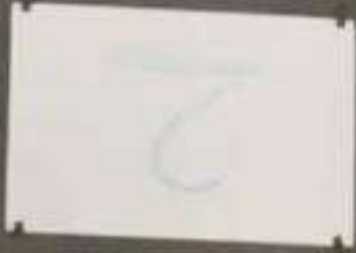
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**Soft  
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**Randomness  
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[D. Fremont et al., “Control Improvisation”, FSTTCS 2015. Extended version on arxiv, 2018.]

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*Control Improvisation* is a precisely-defined theoretical problem capturing these requirements

[D. Fremont et al., “Control Improvisation”, FSTTCS 2015. Extended version on arxiv, 2018.]



# Related Work

- Control improvisation is a **fundamentally new type of problem**

	HARD	SOFT	RANDOM	REACTIVE
Factor Oracles [1]		■		
Mutational Fuzzers [2]		■		
Uniform Sampling [3]	■		■	
Generative Fuzzers [2,3]	■		■	
Reactive Synthesis [4]	■			■
<i>Control Improvisation</i>	■	■	■	■

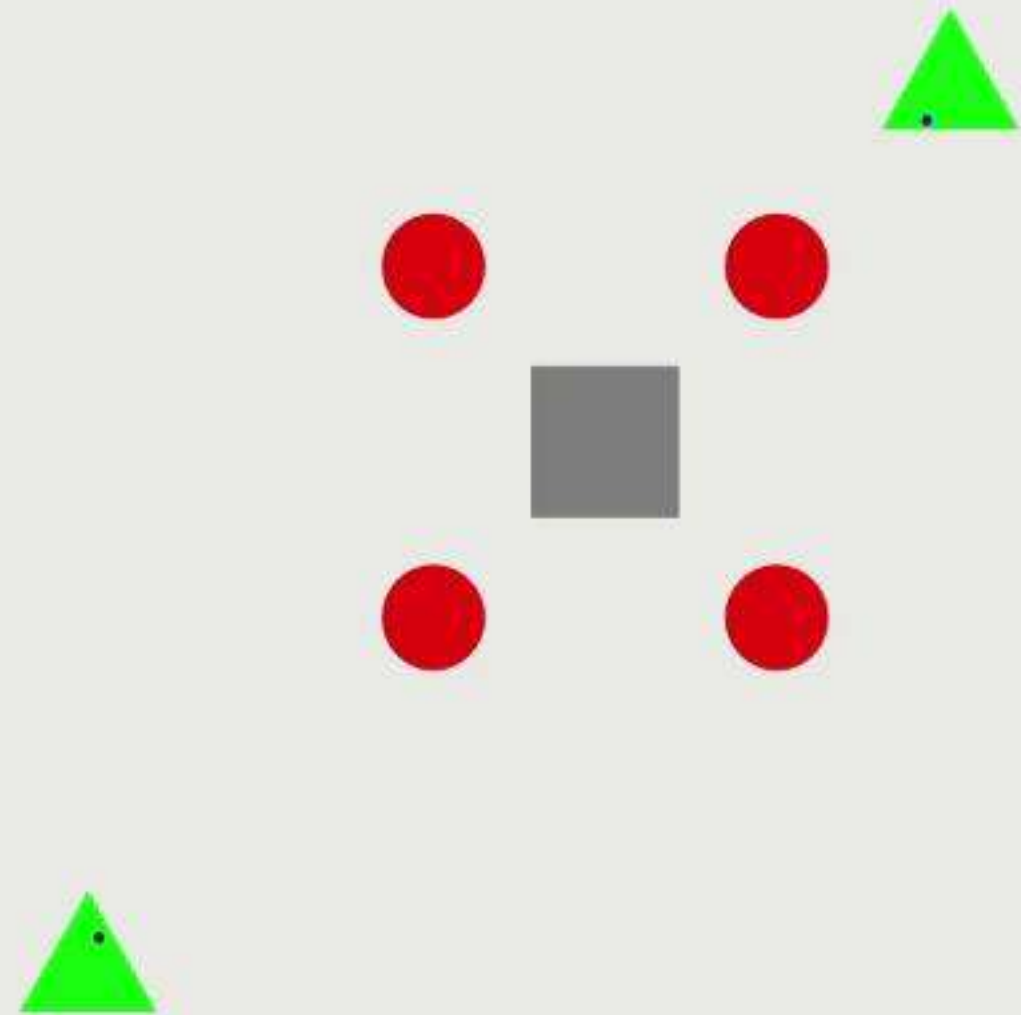
[1] Assayag & Dubnov, *Soft Computation*, 2004.

[2] see Sutton, Greene, & Amini, Addison-Wesley, 2007.

[3] e.g. Hickey & Cohen, *SIAM Journal on Computing*, 1983.

[4] e.g. Pnueli & Rosner, POPL 1989.

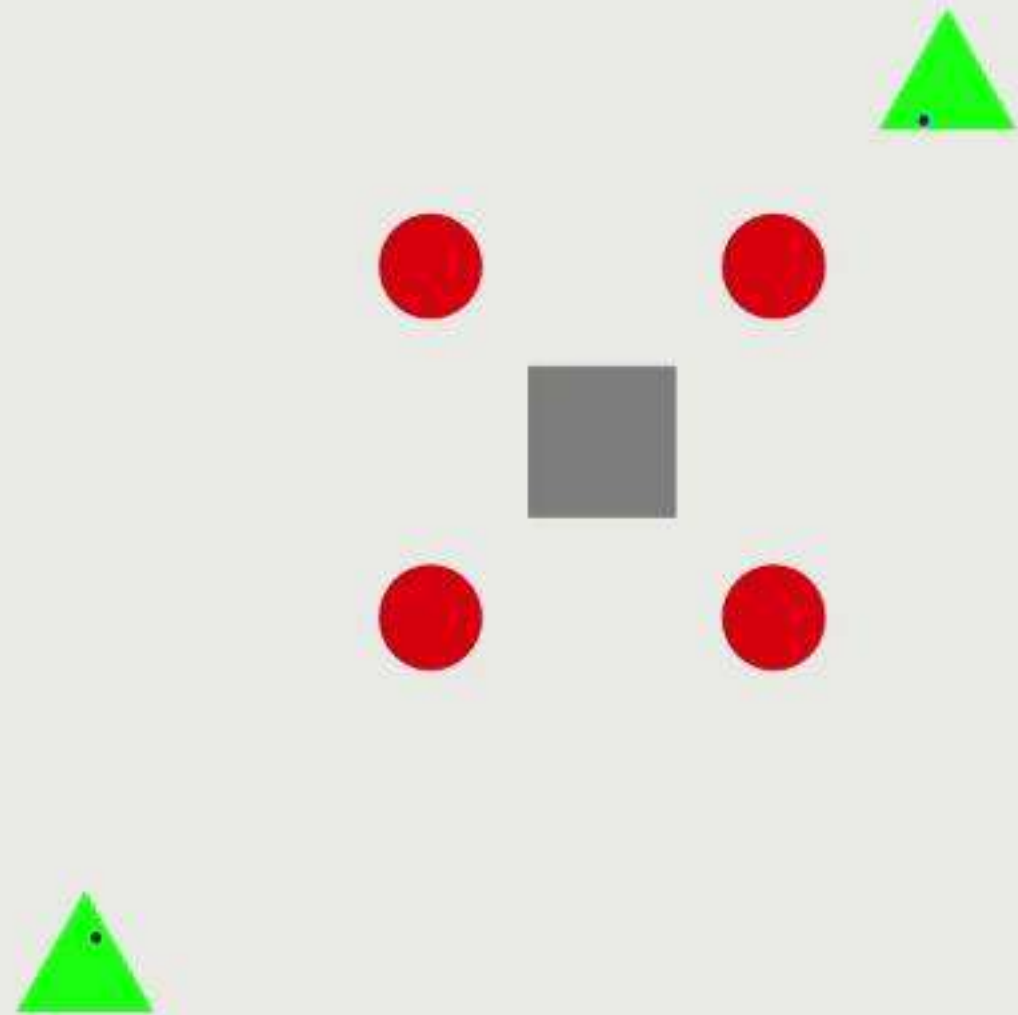
# Components of the Definition





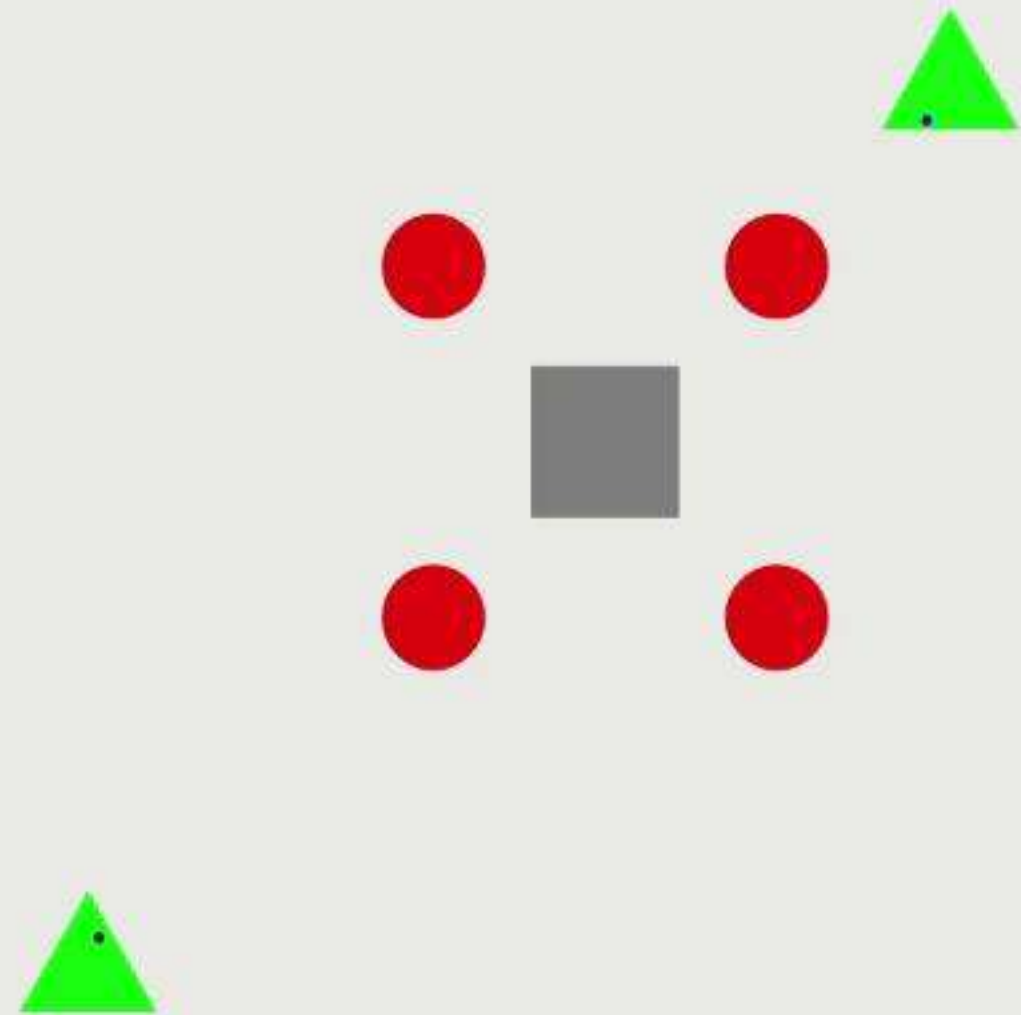
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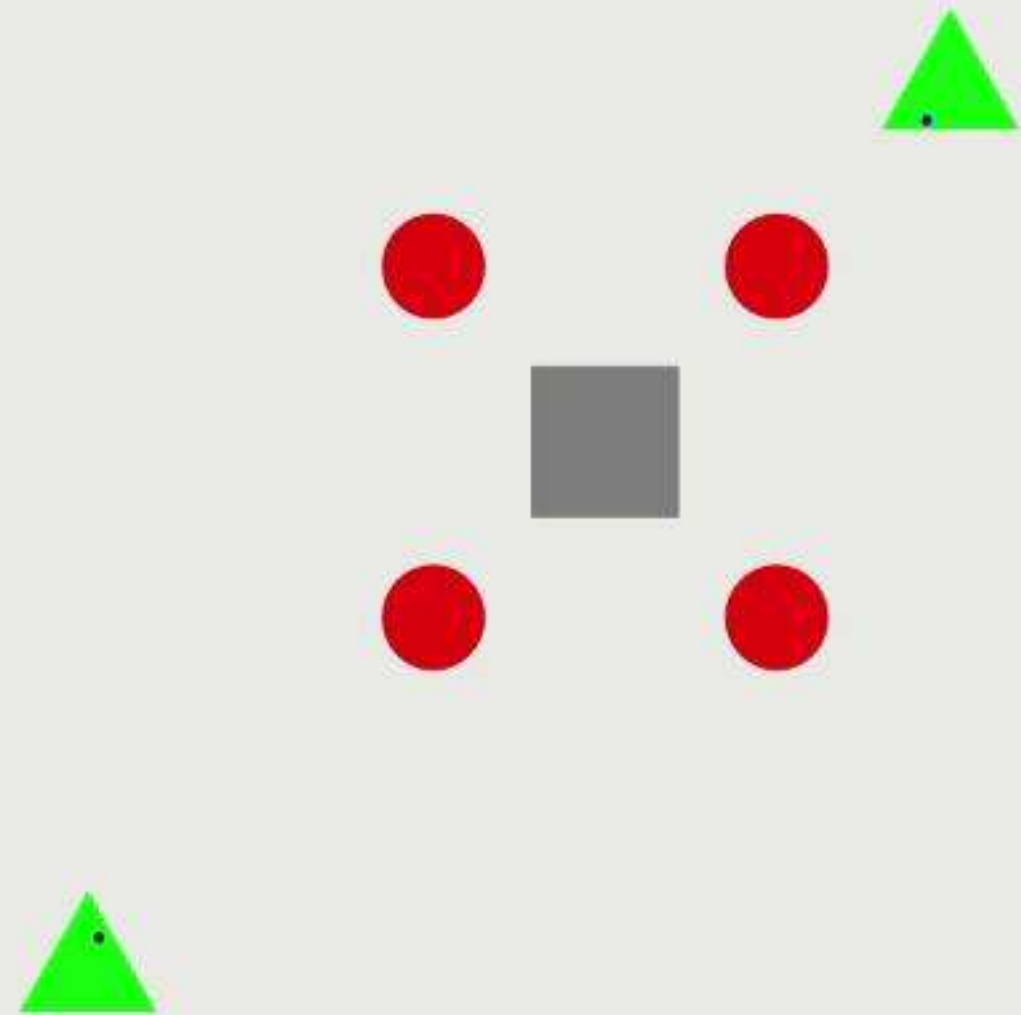
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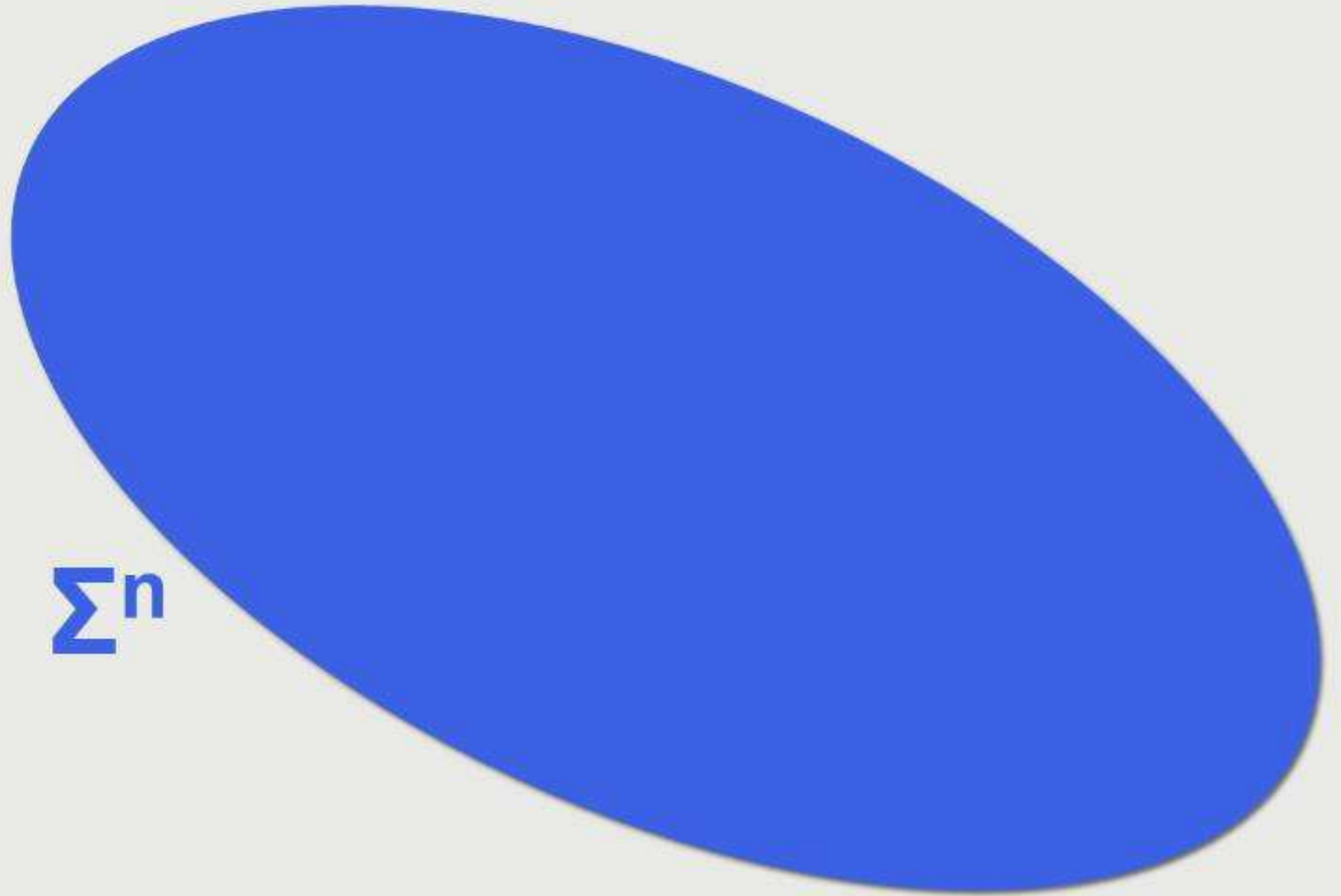


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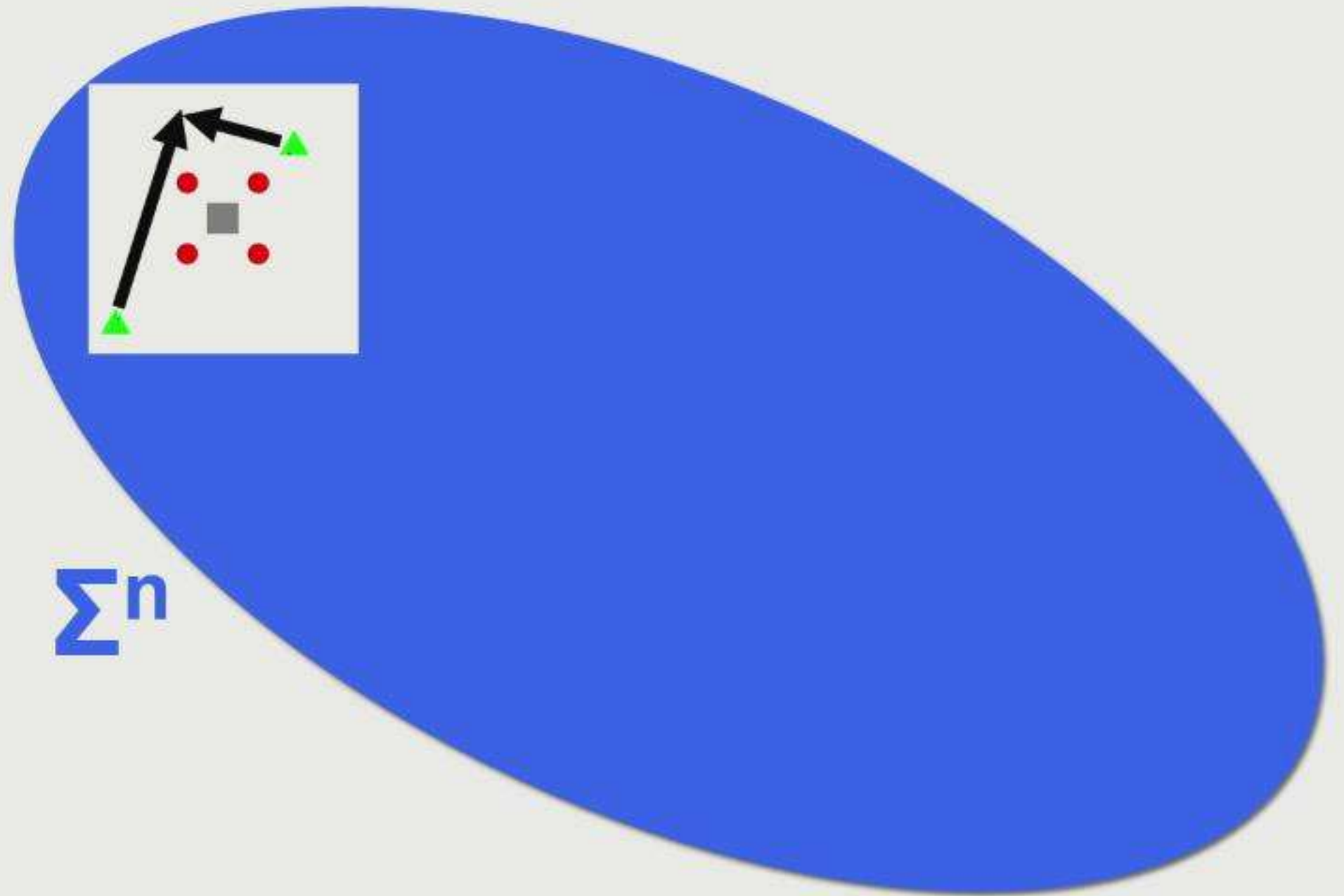
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$\Sigma^n$

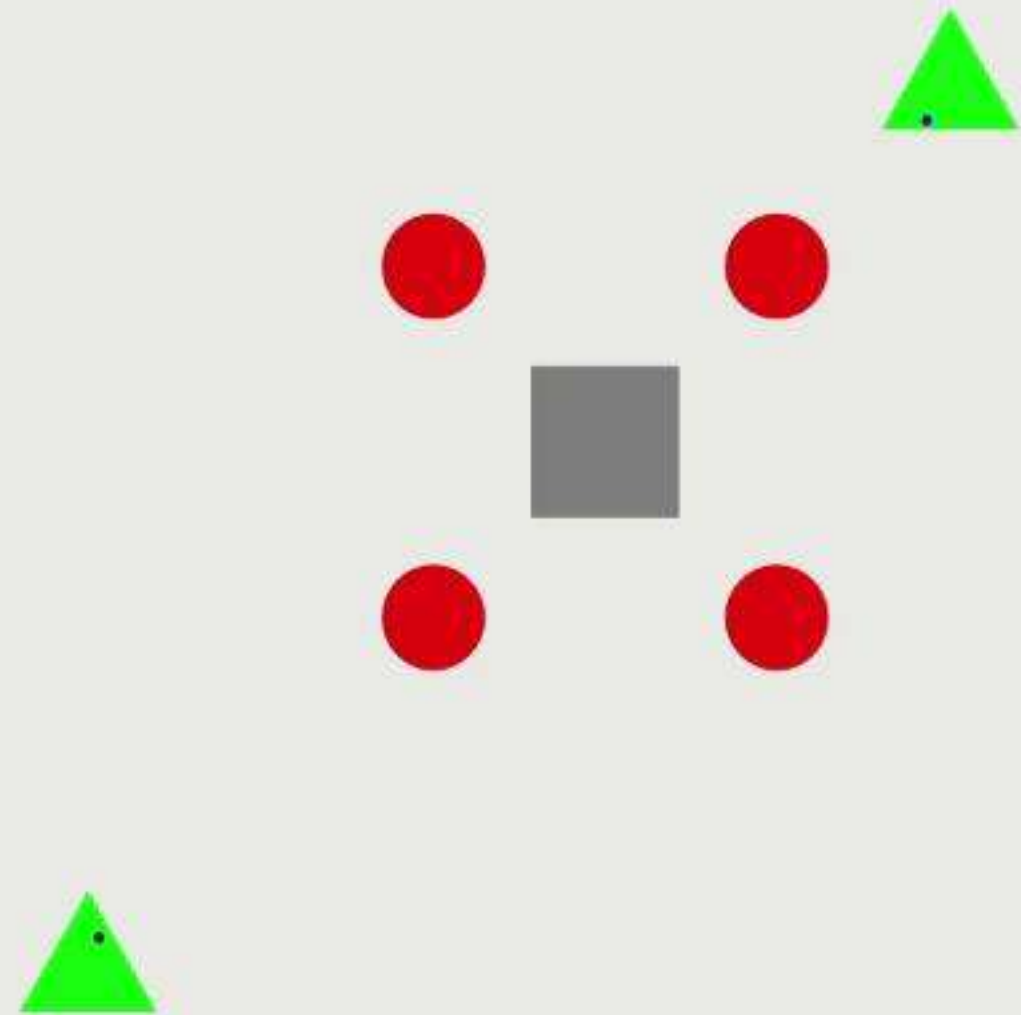


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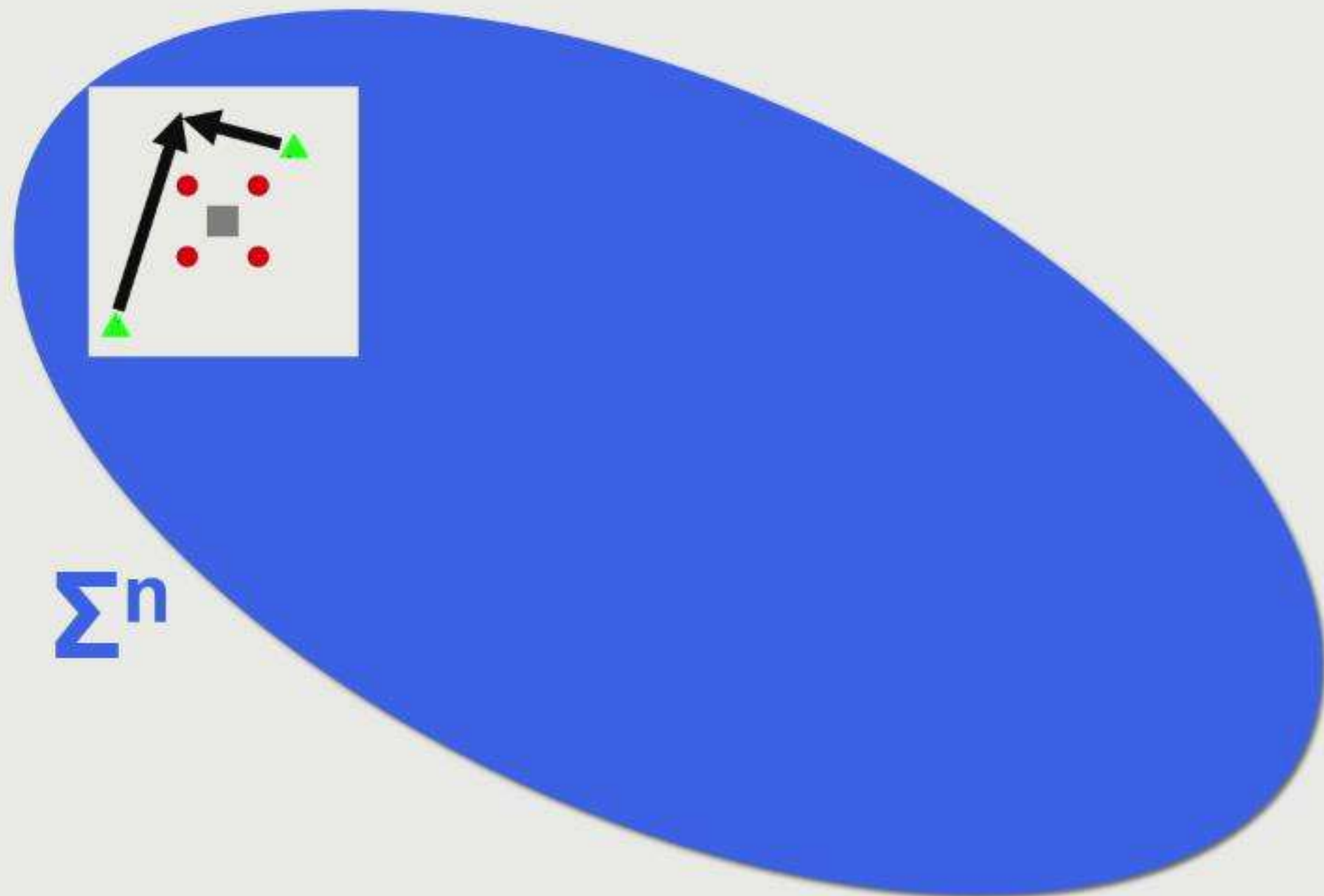
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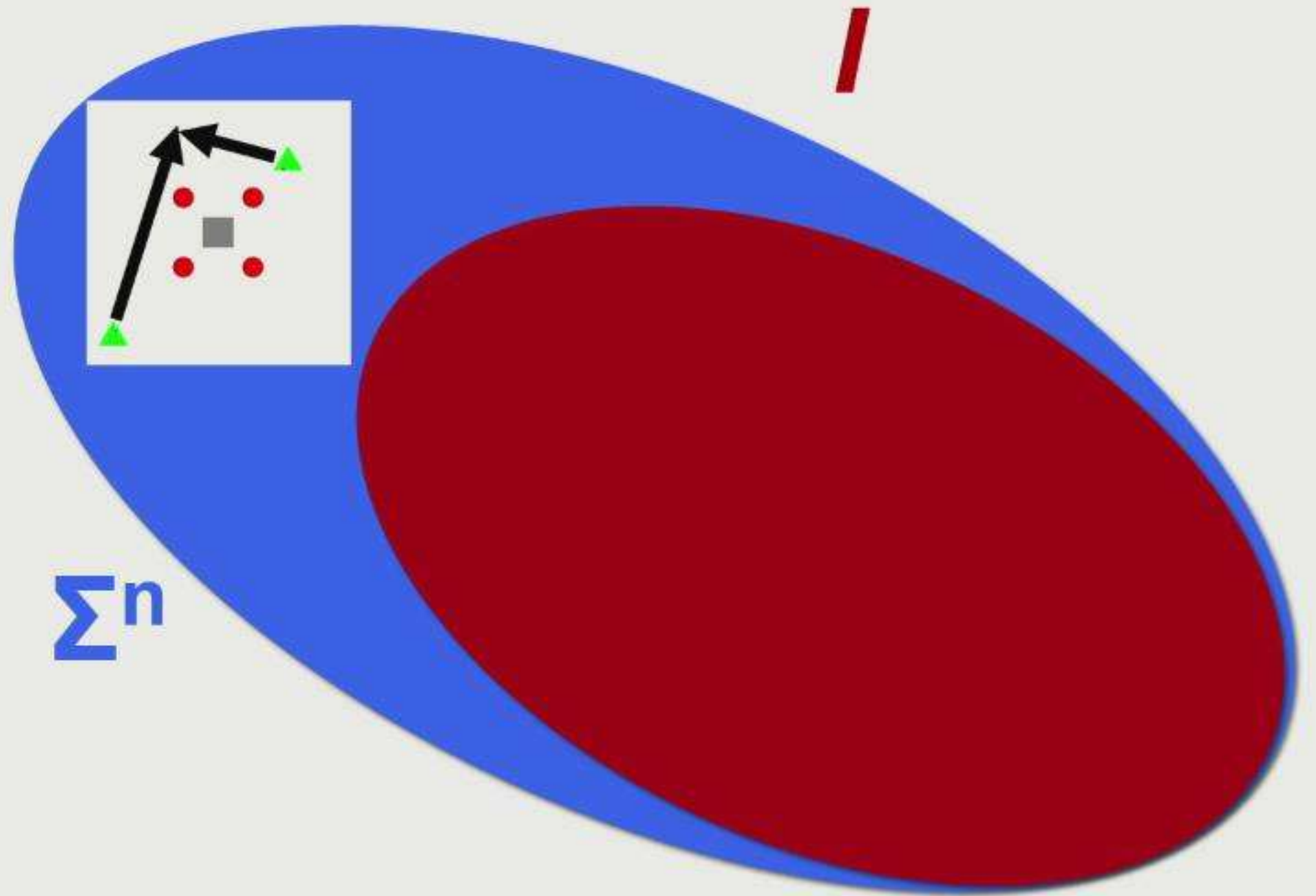


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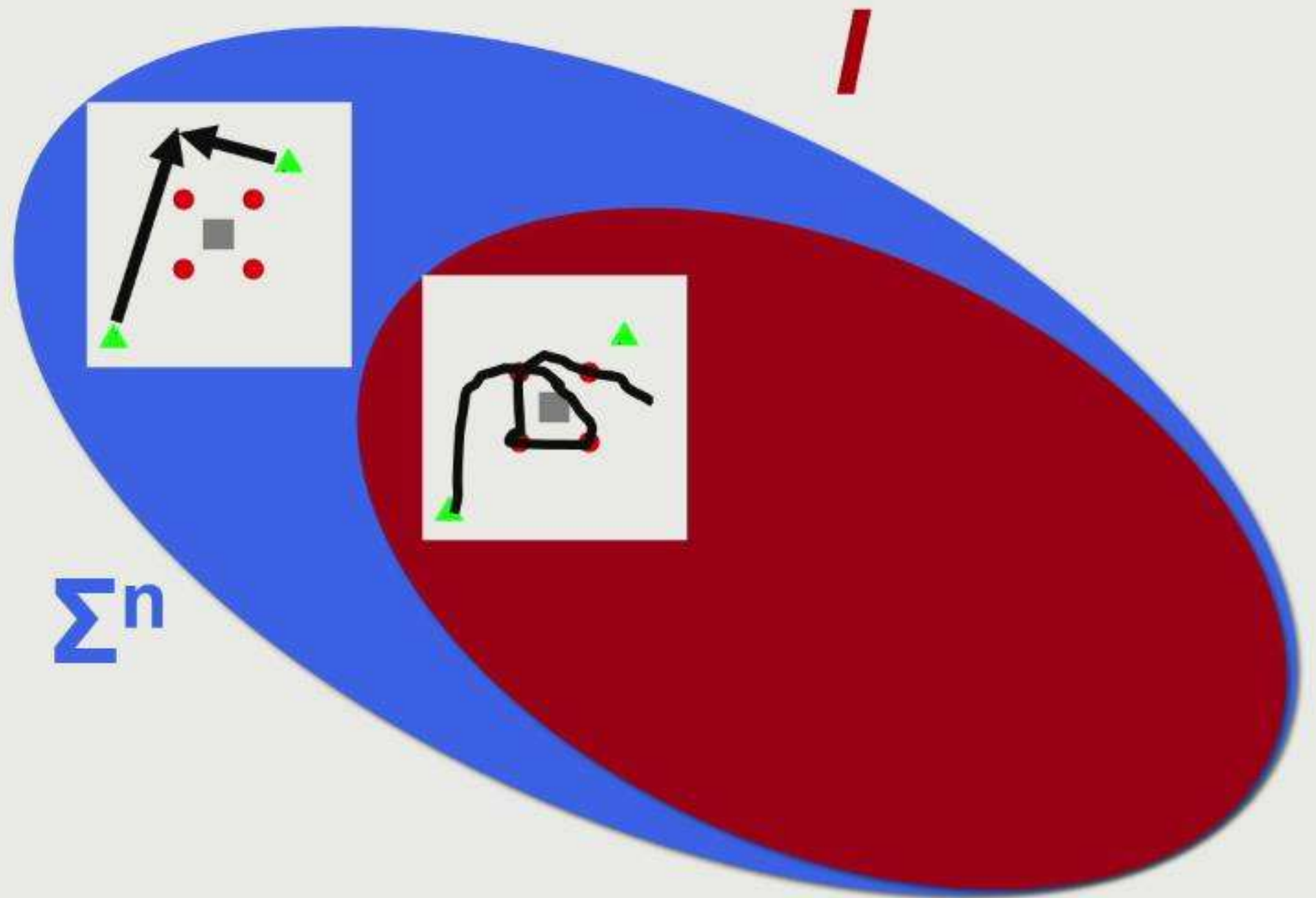
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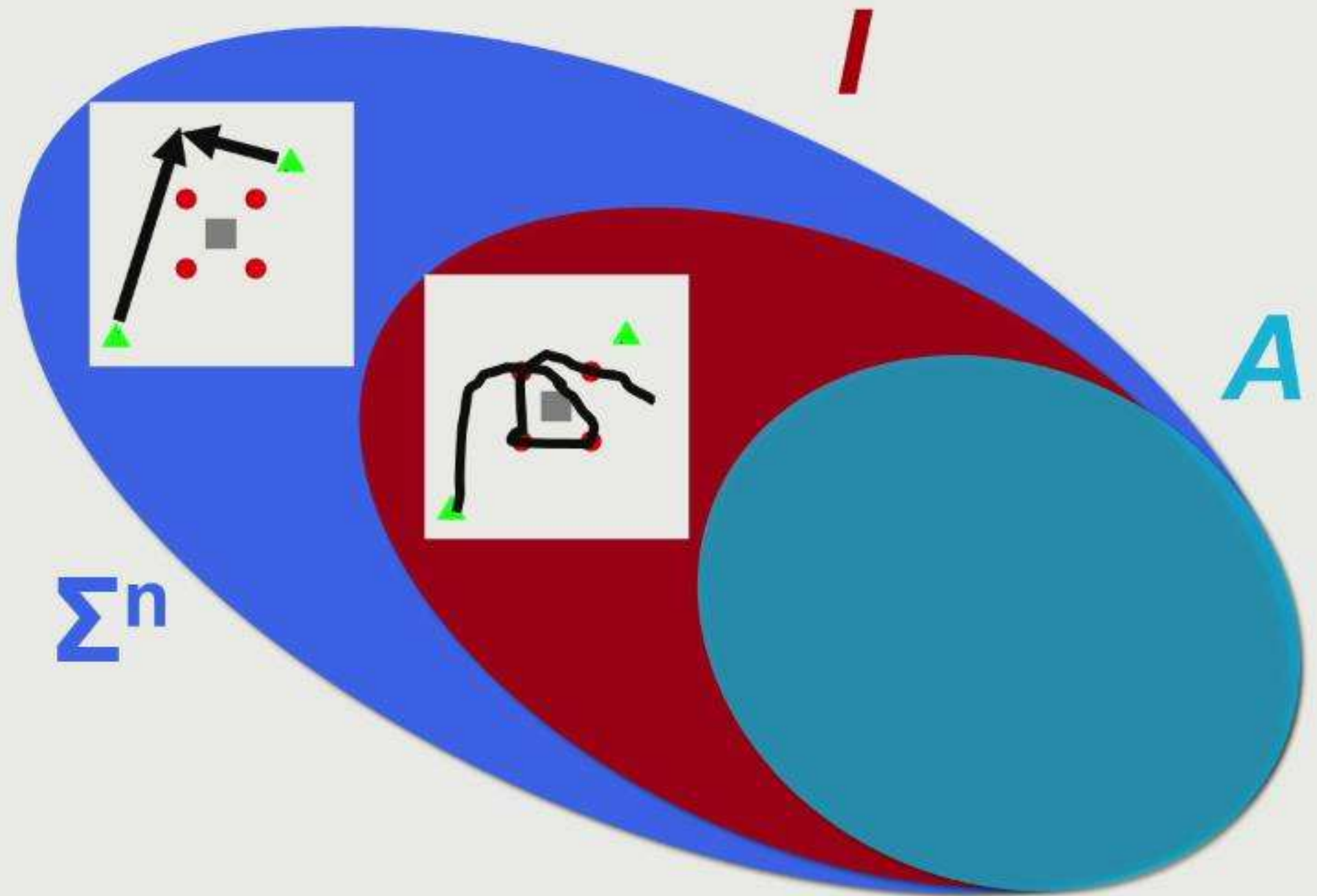
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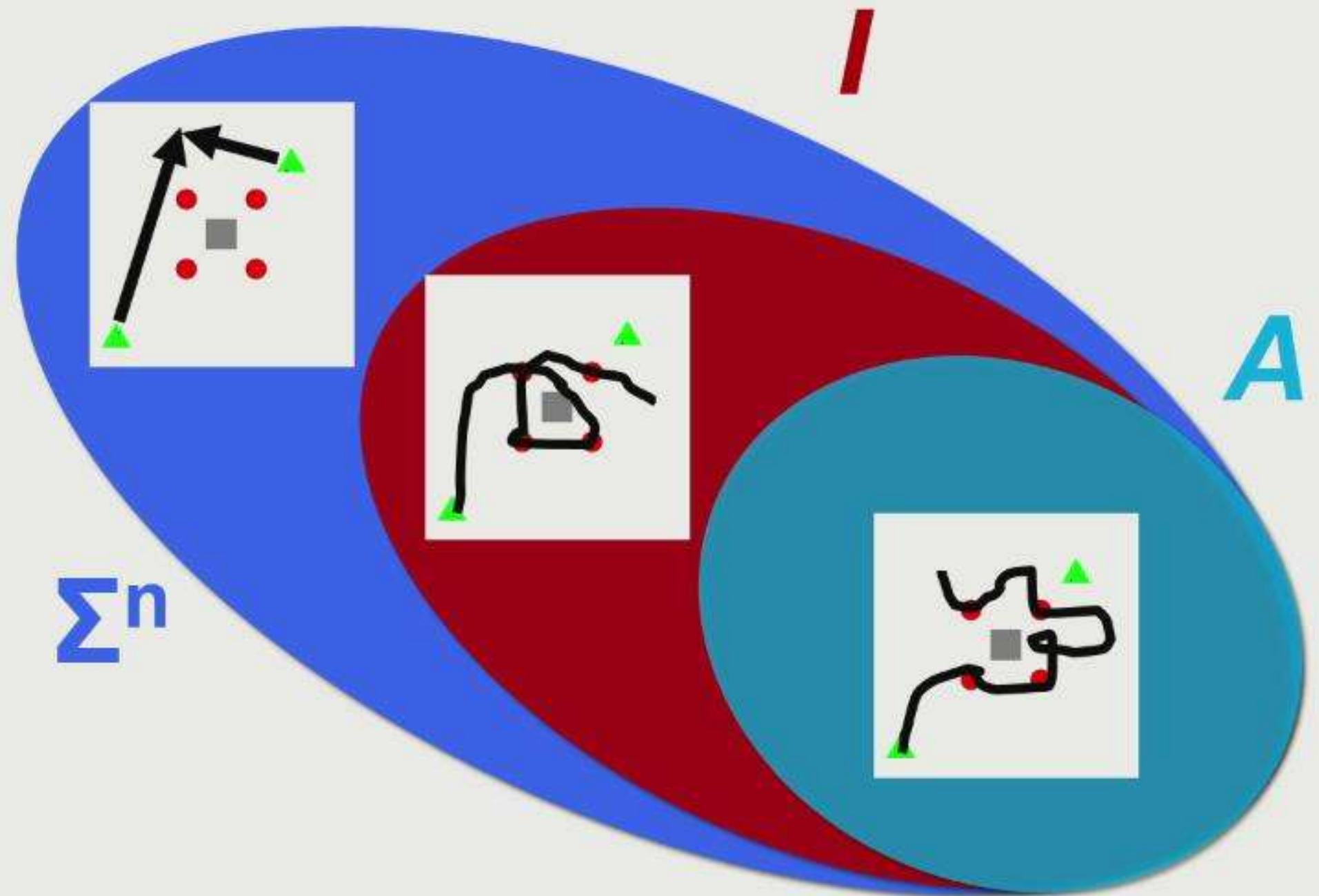
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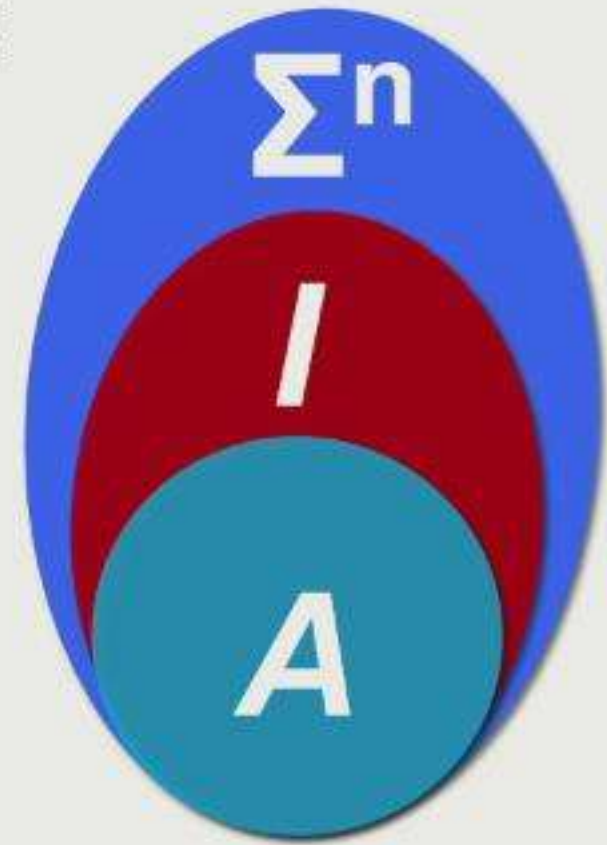
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# Definition of Control Improviser

Given  $H, S, n$ , an *error probability*  $0 \leq \varepsilon \leq 1$ , and bounds  $0 < \lambda, \rho \leq 1$ , a distribution  $D : \Sigma^* \rightarrow [0,1]$  is an *improvising distribution* if:

- 
- 
- 





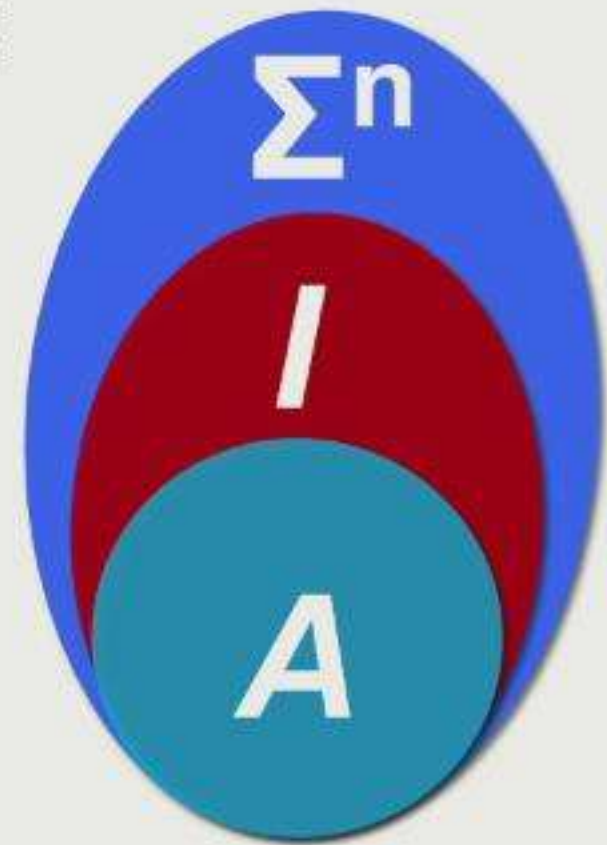
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Hard constraint

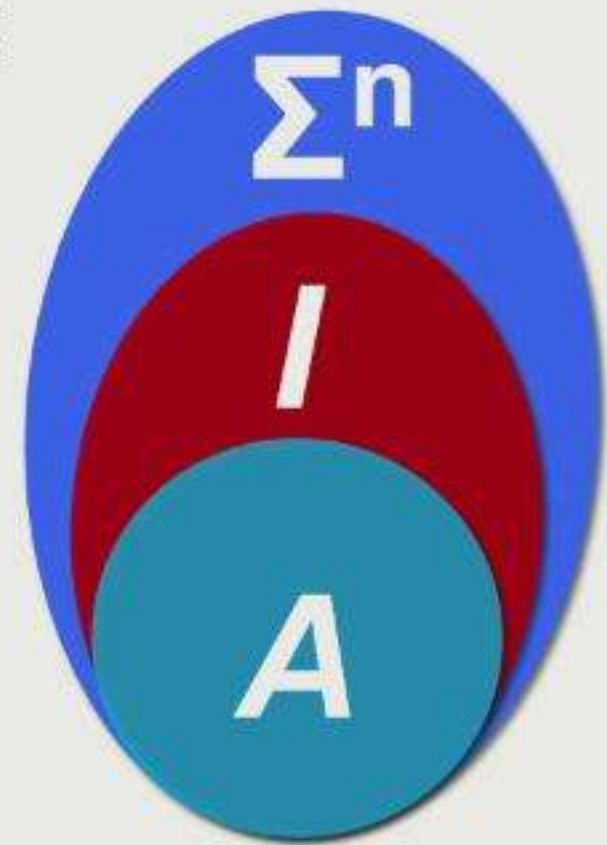
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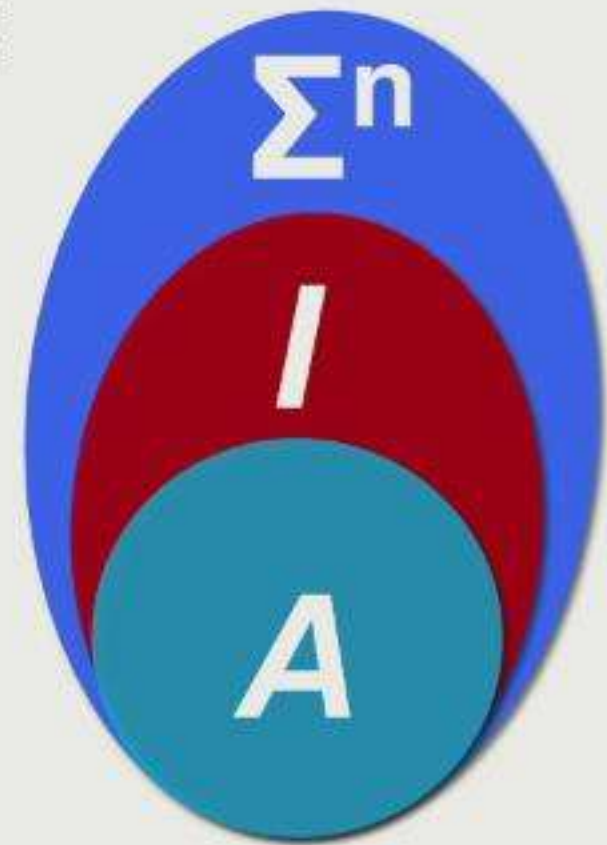




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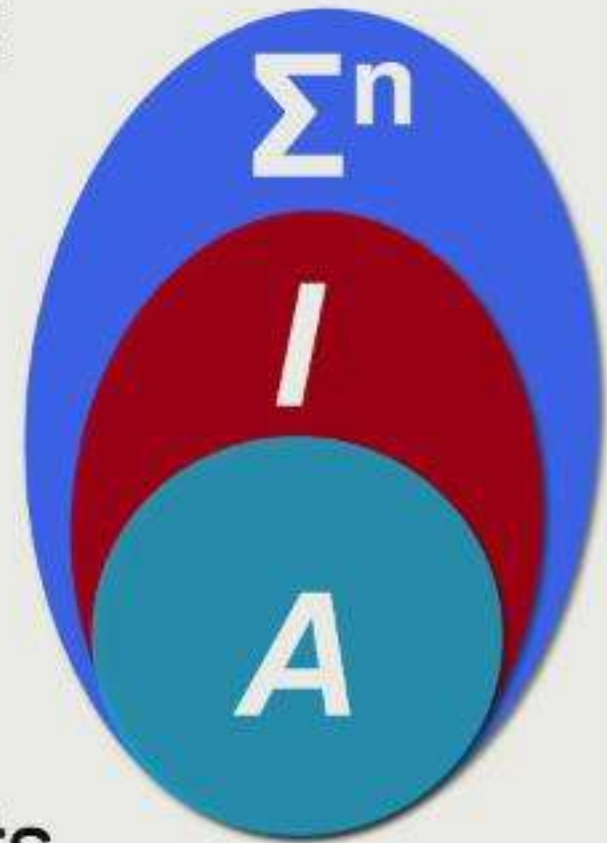
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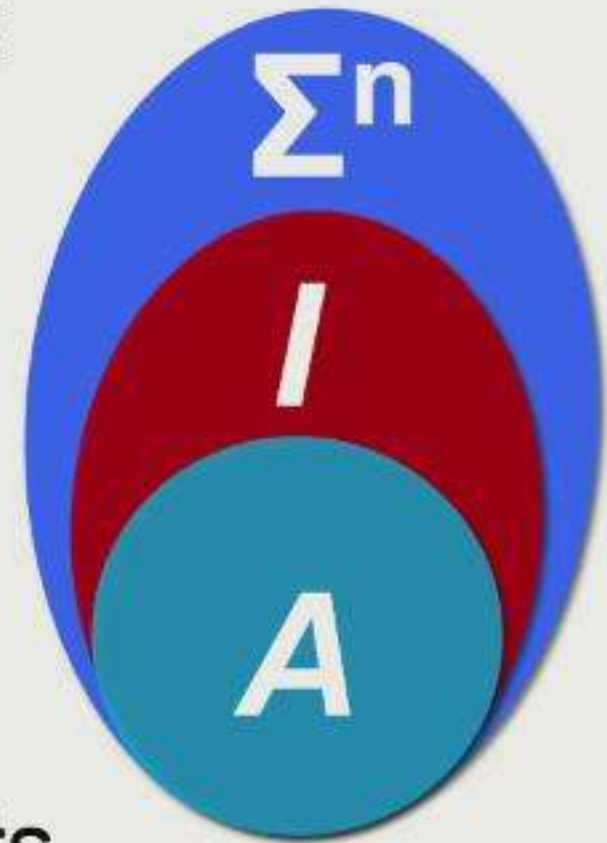
The CI instance  $\mathcal{C} = (\mathcal{H}, \mathcal{S}, n, \varepsilon, \lambda, \rho)$  is *feasible* if  $D$  exists.



# Definition of Control Improviser

Given  $H, S, n$ , an *error probability*  $0 \leq \varepsilon \leq 1$ , and bounds  $0 < \lambda, \rho \leq 1$ , a distribution  $D : \Sigma^* \rightarrow [0,1]$  is an *improvising distribution* if:

- $\Pr[w \in I \mid w \leftarrow D] = 1$  **Hard constraint**
- $\Pr[w \in A \mid w \leftarrow D] \geq 1 - \varepsilon$  **Soft constraint**
- $\forall w \in I, \lambda \leq D(w) \leq \rho$  **Randomness req.**

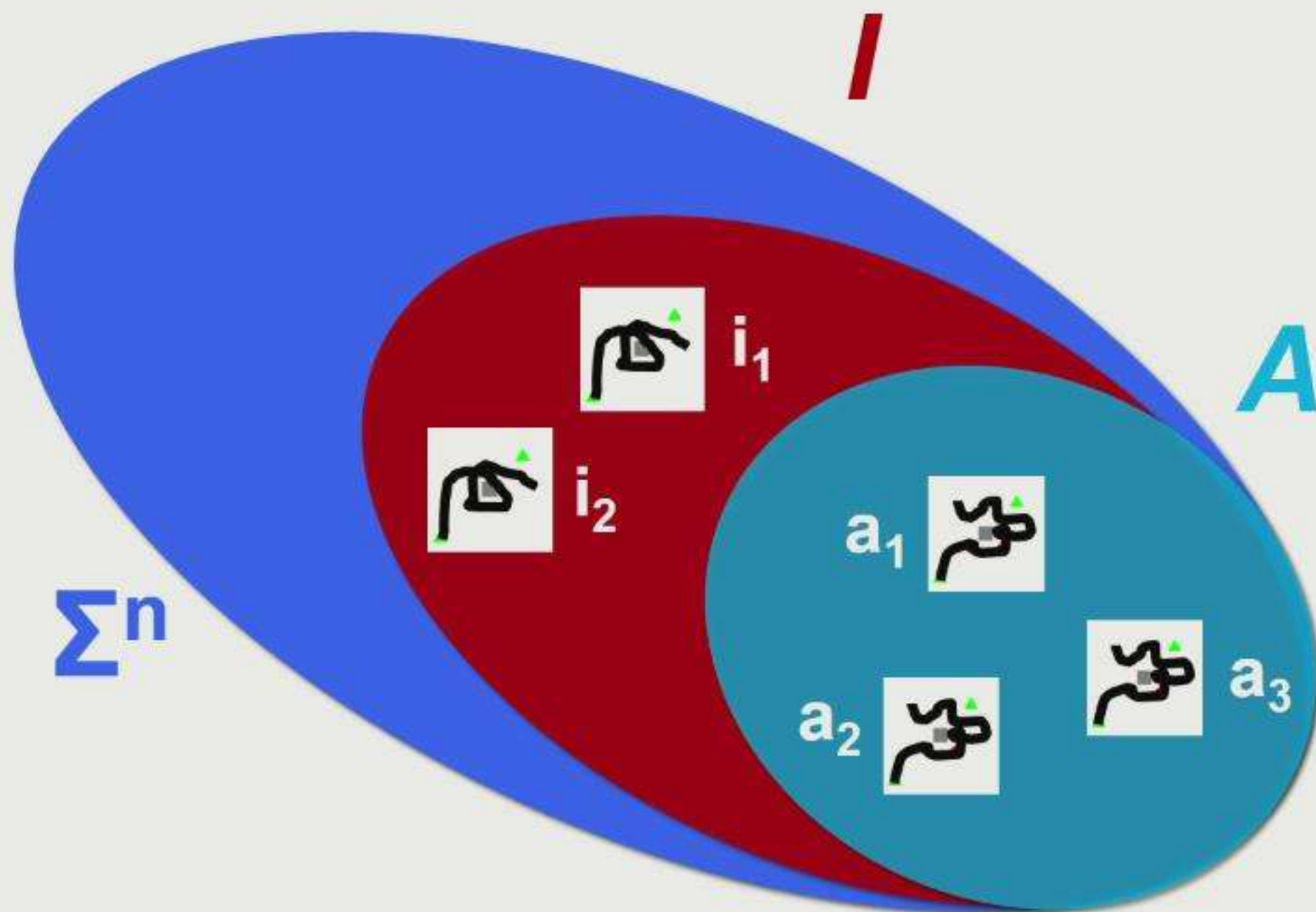


The CI instance  $\mathcal{C} = (\mathcal{H}, \mathcal{S}, n, \varepsilon, \lambda, \rho)$  is *feasible* if  $D$  exists.

An *improviser* is a probabilistic algorithm sampling from  $D$ .

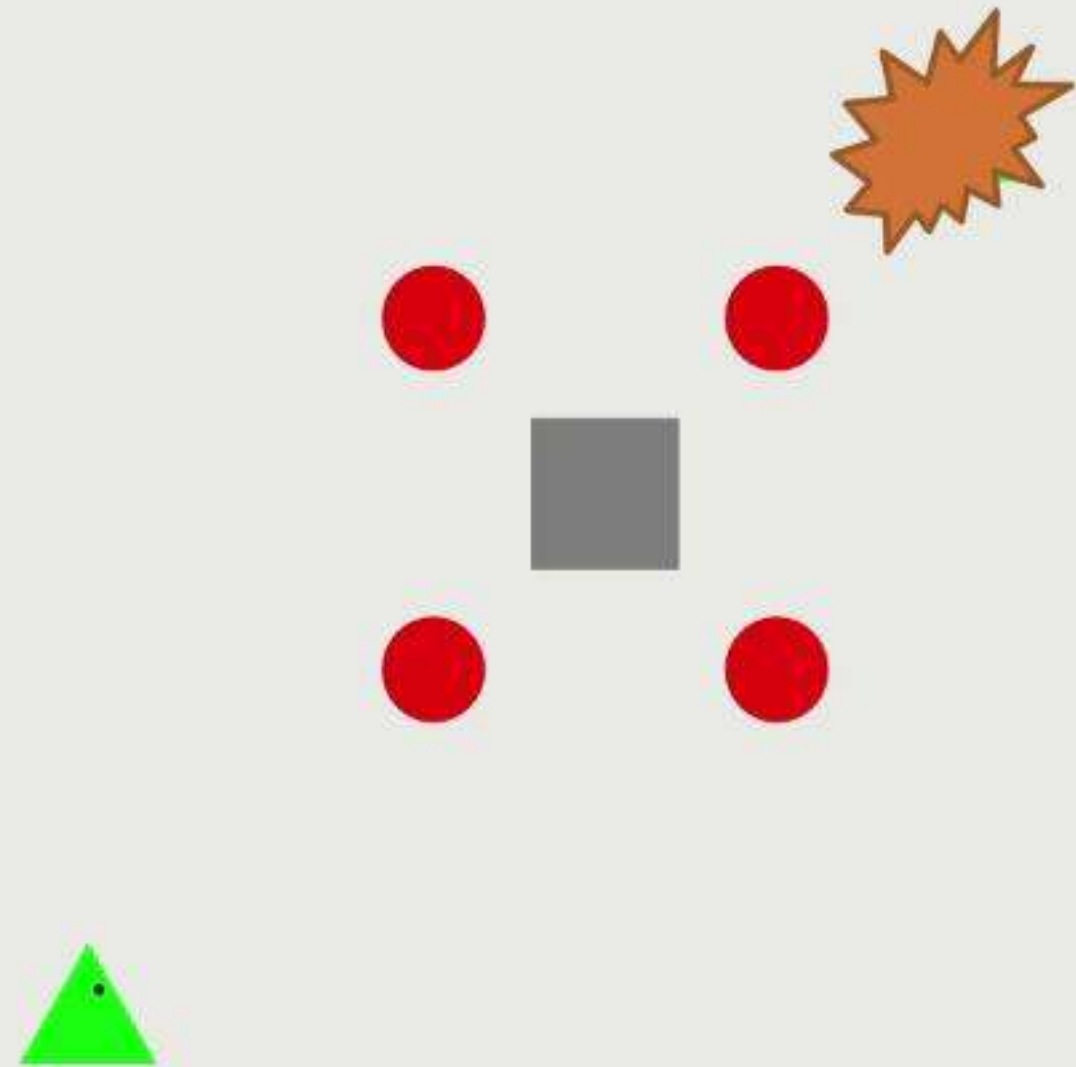
# Example

- Suppose  $A = \{a_1, a_2, a_3\}$   
and  $I \setminus A = \{i_1, i_2\}$
- With  $\varepsilon = \rho = 1/4$ :
  - Return  $a_1, a_2,$  and  $a_3$  with probability  $1/4$
  - Return  $i_1$  and  $i_2$  with probability  $1/8$





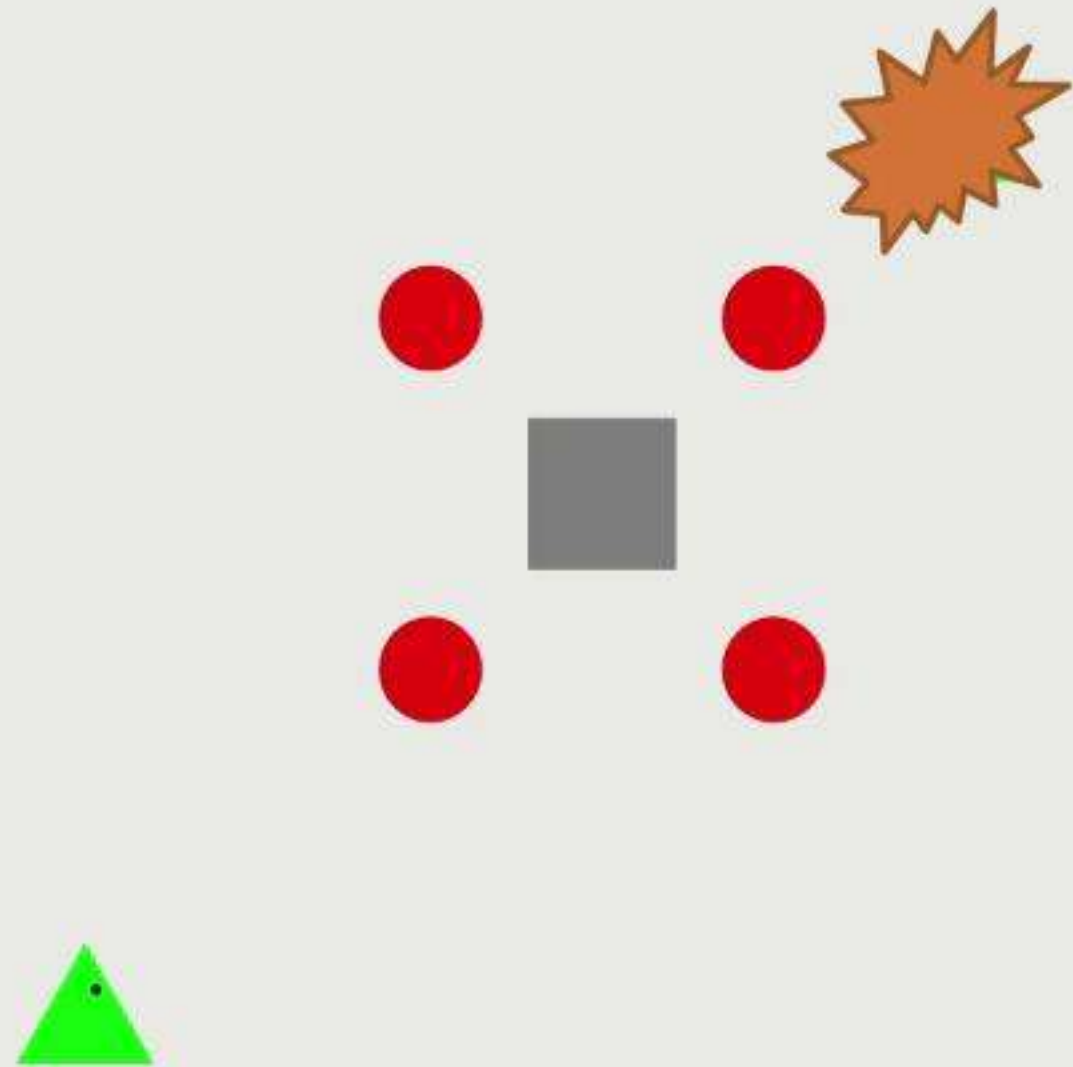
# Reactive Control Improvisation



Fremont and Seshia, *Reactive Control Improvisation*, CAV 2018.

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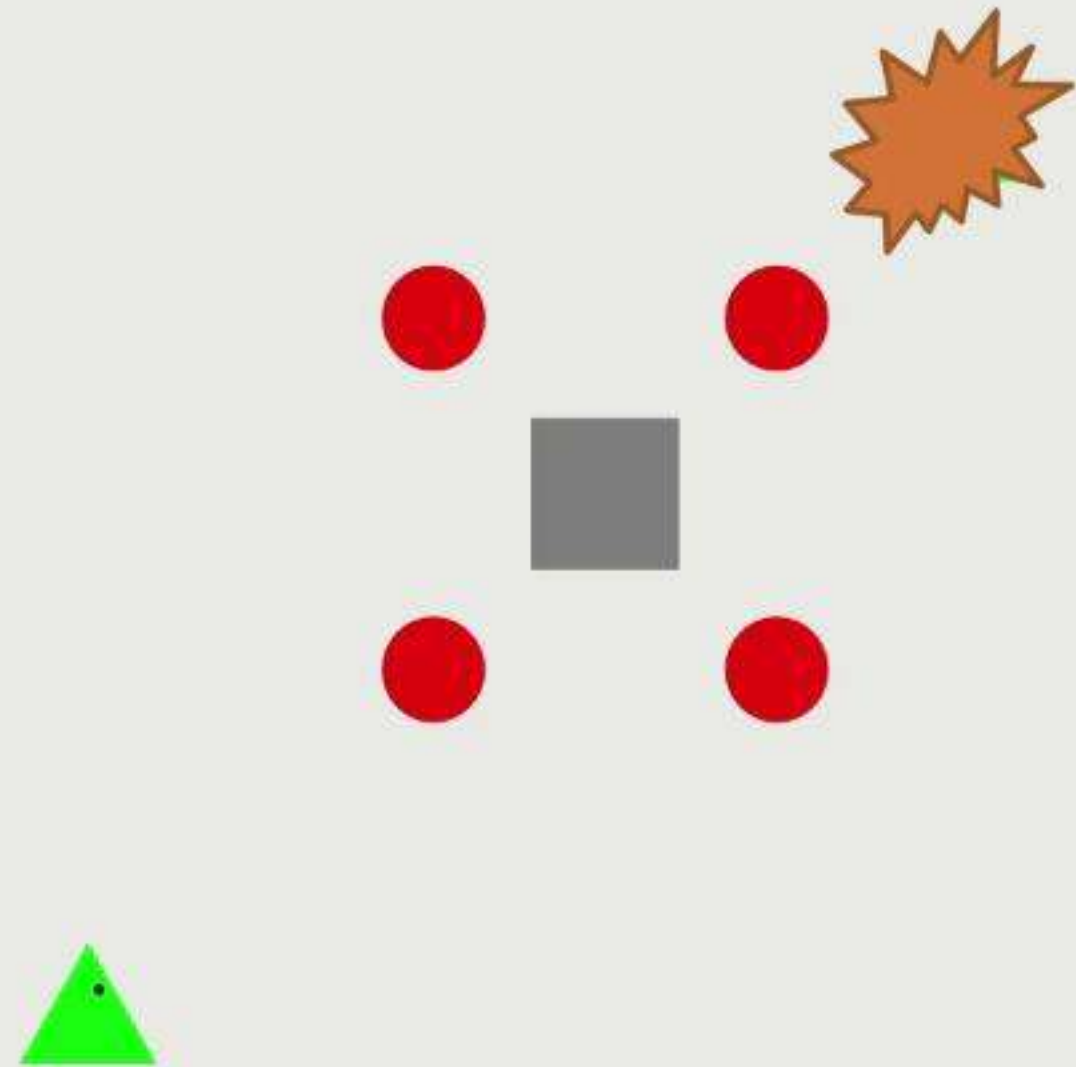
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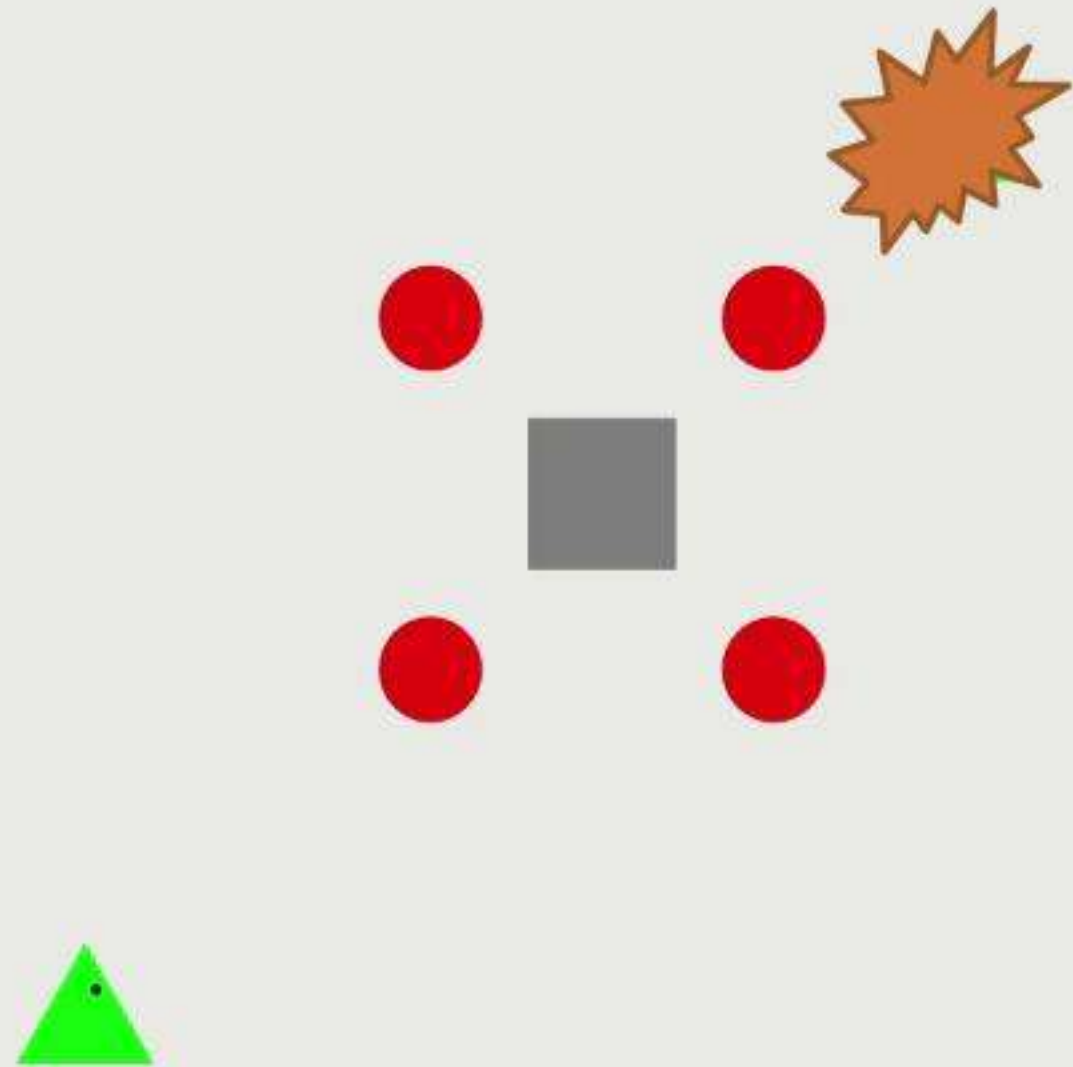
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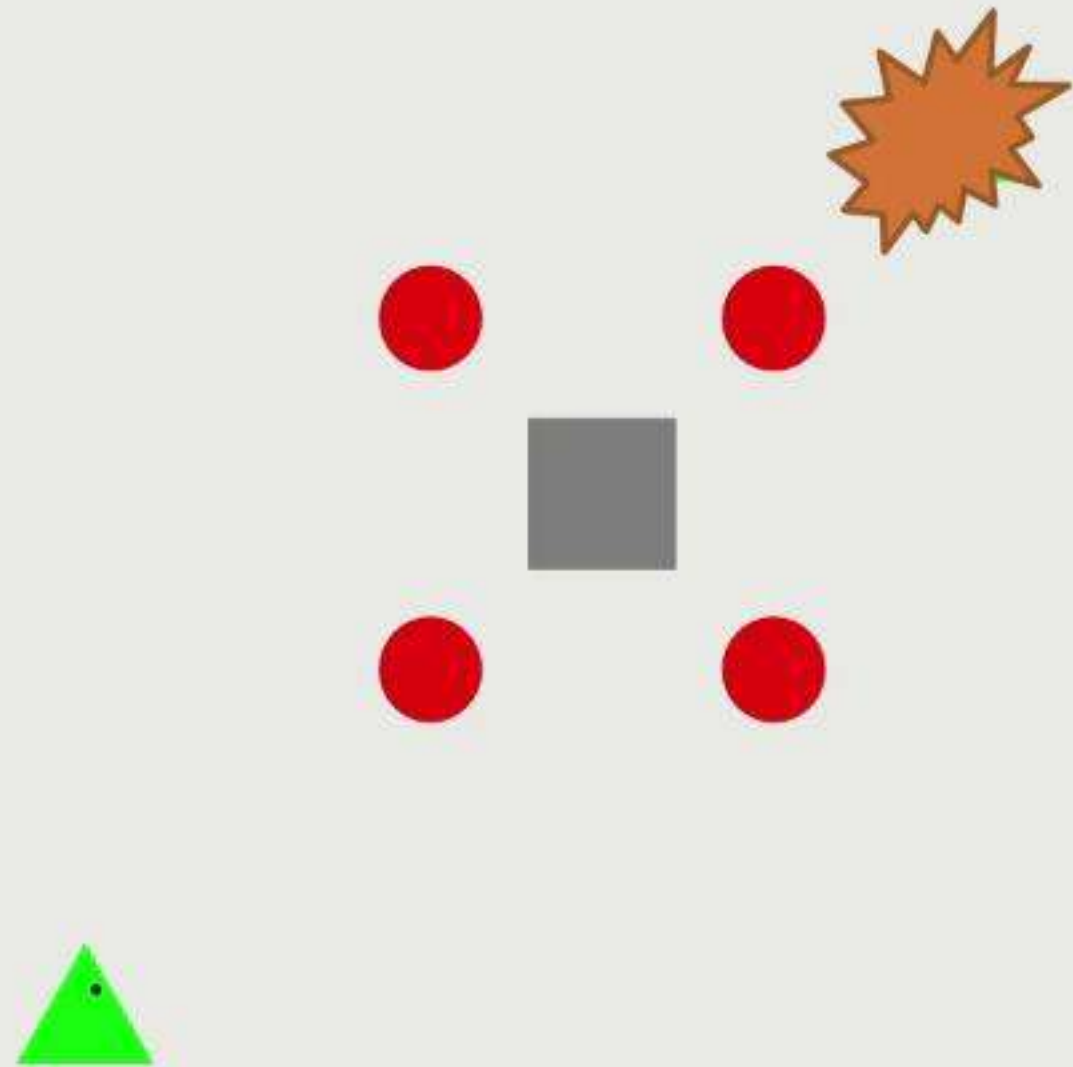
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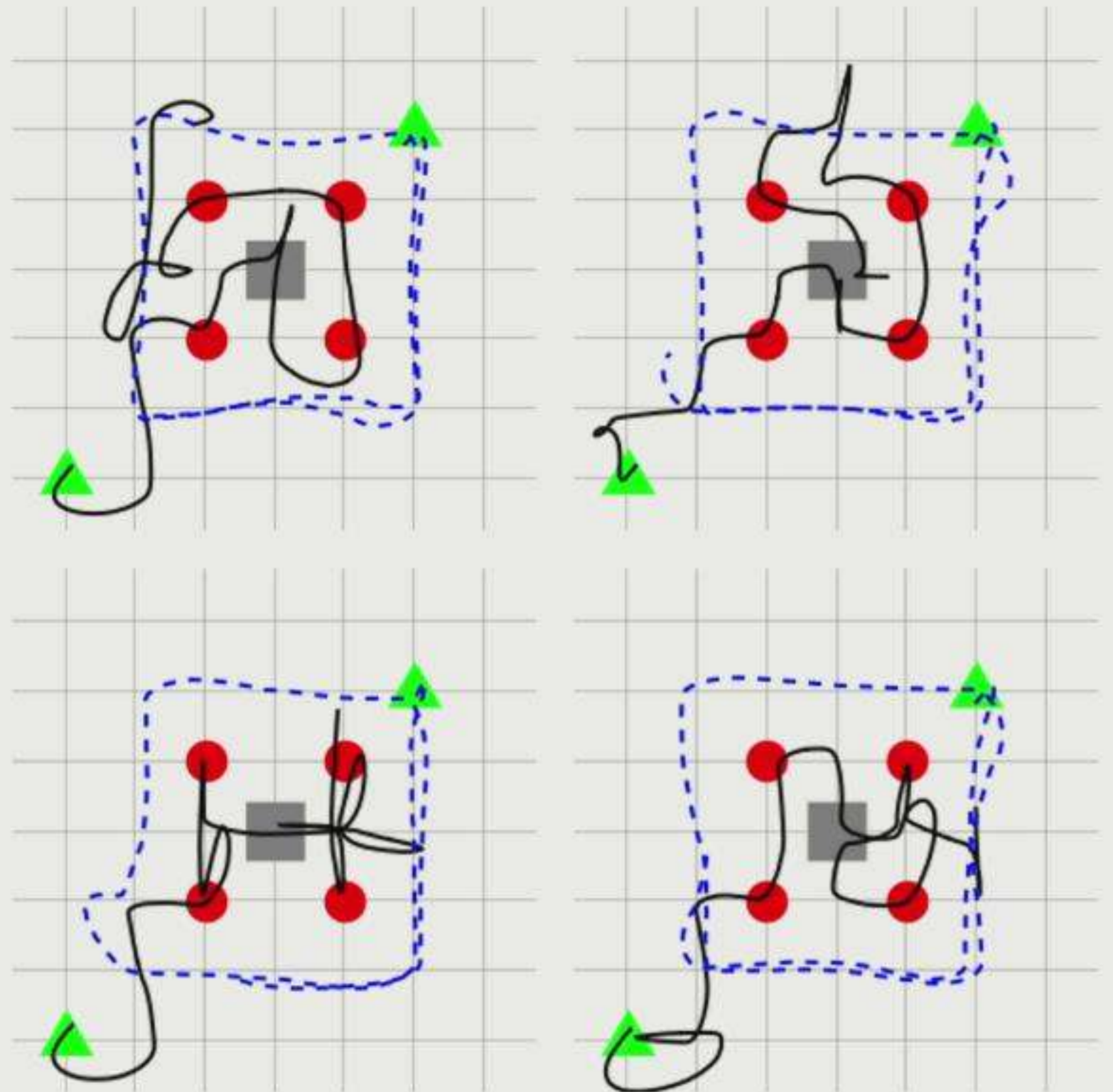
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  - System and adversary alternate picking symbols (2-player game)
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  - Improviser → improvising *strategy*
- This enables randomized reactive synthesis (for bounded time)



# RCI Example

- Hard constraint:
  - Visit the 4 circles in 30 moves, avoiding the adversary
- Soft constraint:
  - 75% of the time, visit each circle exactly once
- Randomness requirement:
  - Use the smallest feasible  $\rho$  (about  $10^{-12}$ )





# Outline

1. Control Improvisation
  - Definition and motivating applications
2. **Theory of CI**
  - Efficient algorithms and hardness results
3. Designing and Analyzing Perception Systems
4. Conclusion & Future Work

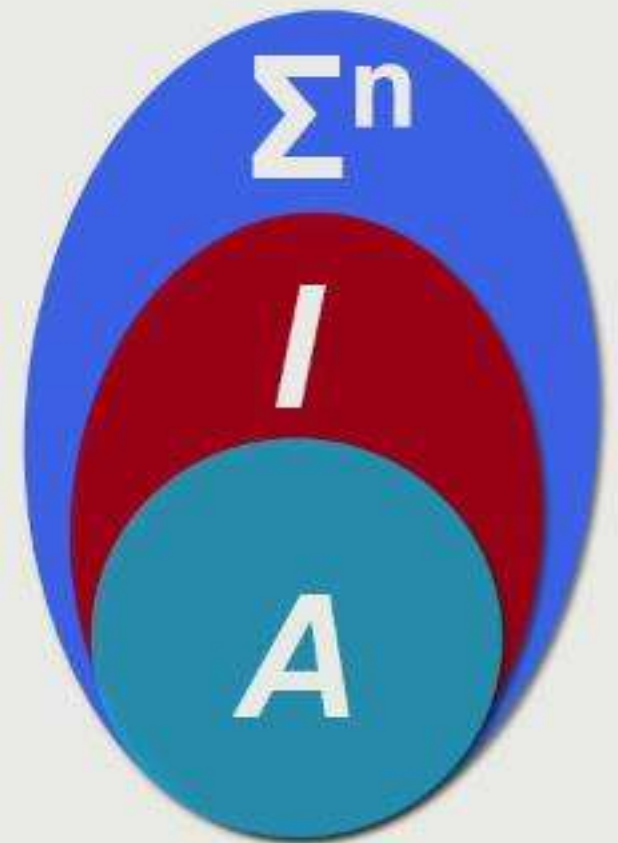
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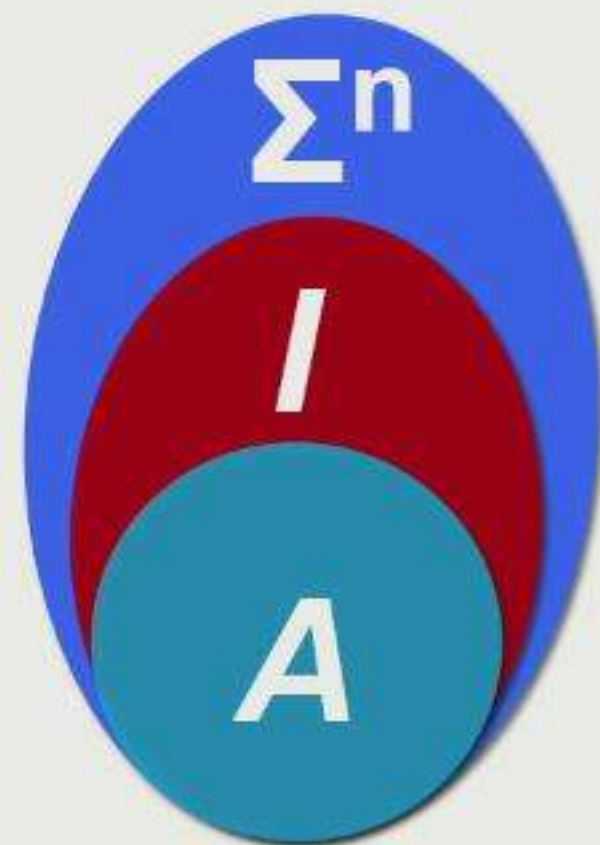


# Existence of Improvisers

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**Theorem.** A CI instance  $\mathcal{C} = (H, S, n, \epsilon, 0, \rho)$  is feasible if and only if:

- $|I| \geq 1/\rho$
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# Improvisation Schemes

A synthesis algorithm:



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*A polynomial-time improvisation scheme* for a class  $P$  of CI instances is an algorithm  $S$  such that given  $C$  in  $P$ ,



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- $S$  and the improvisers it generates run in time polynomial in  $|C|$

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    3. Sample from  $A$  or  $I \setminus A$  with the right probabilities

# Algorithms and Complexity

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$\mathcal{H}$	$S$	DFA	CFG		NFA
			unamb.	amb.	
DFA		poly-time	poly-time	#P	
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	ambiguous				
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Fremont et al., *Control Improvisation*, arXiv:1704.06319, extending FSTTCS 2015.

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- Approximate scheme for Boolean formulas, using SAT solvers

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**Theorem.** An RCI instance is feasible if and only if:

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Improviser  
strategy

Adversary  
strategy

Probability of  
obtaining trace  $w$

Number of possible  
traces in  $X$



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- Again, efficient scheme for DFA specifications

$\mathcal{H} \setminus \mathcal{S}$	RSG	DFA	NFA	CFG	LTL	LDL
RSG	poly-time		PSPACE			
DFA						
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- Again, efficient scheme for DFA specifications
- PSPACE-equivalent for temporal logics

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# Motivating Example: an Autonomous Vehicle

- At any moment in time, the *scene* is the environment configuration (object positions, colors, etc.)
- Collecting examples of real-world scenes is expensive
- We would like to generate realistic scenes automatically for training or testing





# Generating Meaningful Scenes

- Scene space is large, high-dimensional



Car Model



Car Location



Car Orientation



Number of Cars



Reference



Scene Background



Car Color



Weather



Time of Day



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- Scene space is large, high-dimensional
- Realistic scenes have complex geometric constraints
- We may be interested in particular types of scenes (e.g. highway traffic)
- Generating these is another instance of CI, but with what kind of specification?



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# Specifications for Scenes

- Again, hard, soft, randomness constraints:
- Objects should not intersect
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- Objects should not intersect
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- The gap between cars should follow this distribution...
- How to encode these? *A probabilistic programming language*





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- Defines a *distribution over scenes*

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Bumper-to-Bumper Traffic  
(~20 lines of Scenic)



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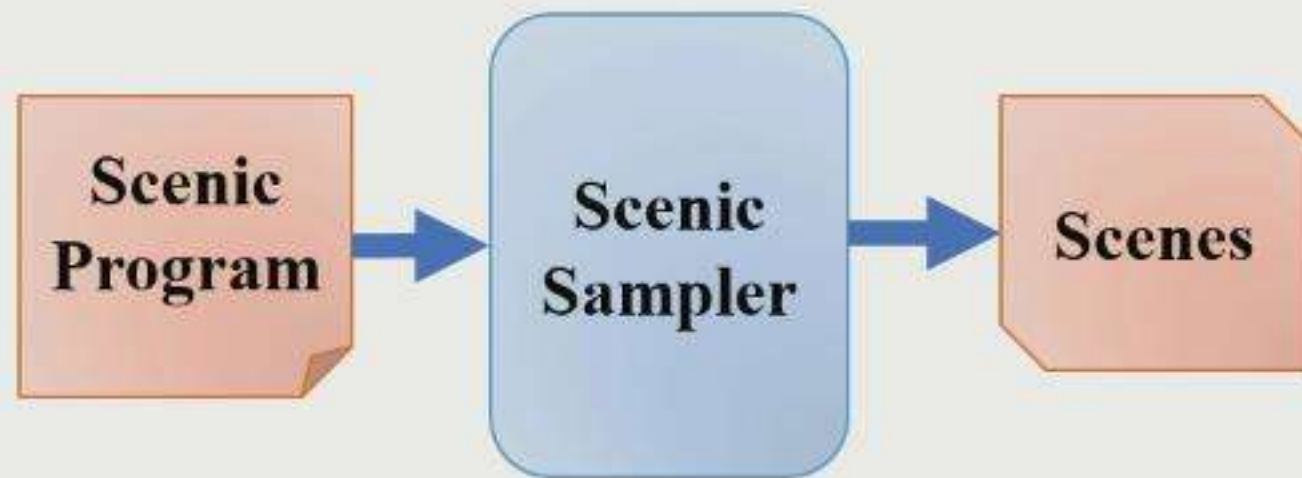
# Designing and Analyzing Systems using a PPL

**Scenic  
Program**

**parkedCar.sc**

```
ego = Car  
Car offset by ...,  
facing ...
```

# Designing and Analyzing Systems using a PPL



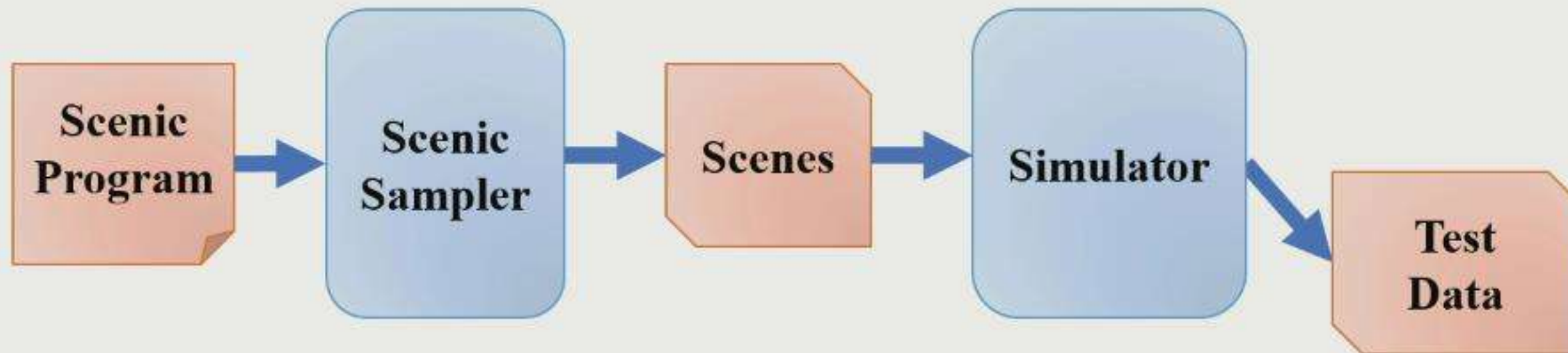
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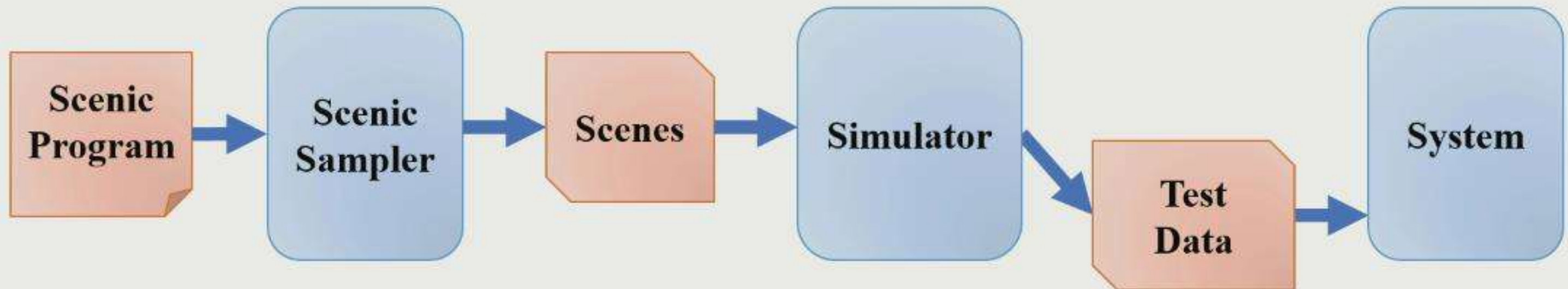


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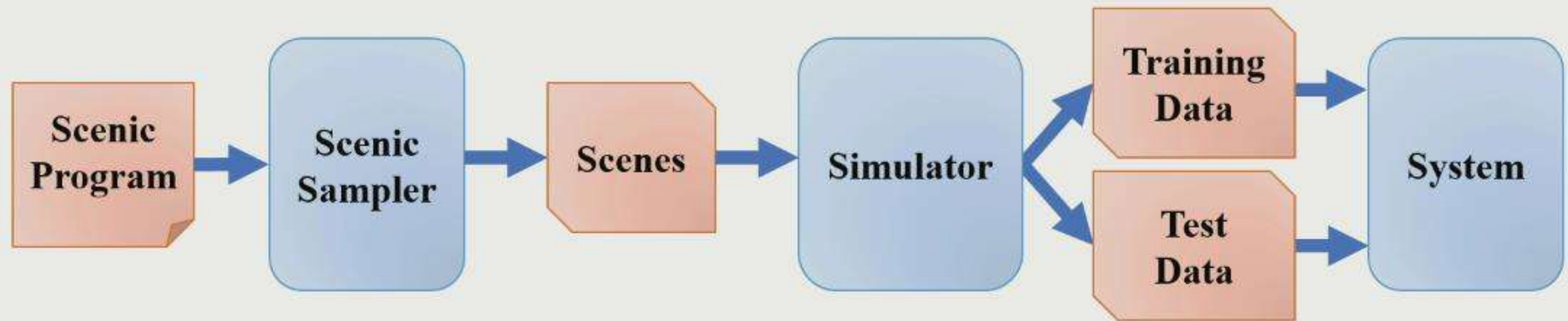
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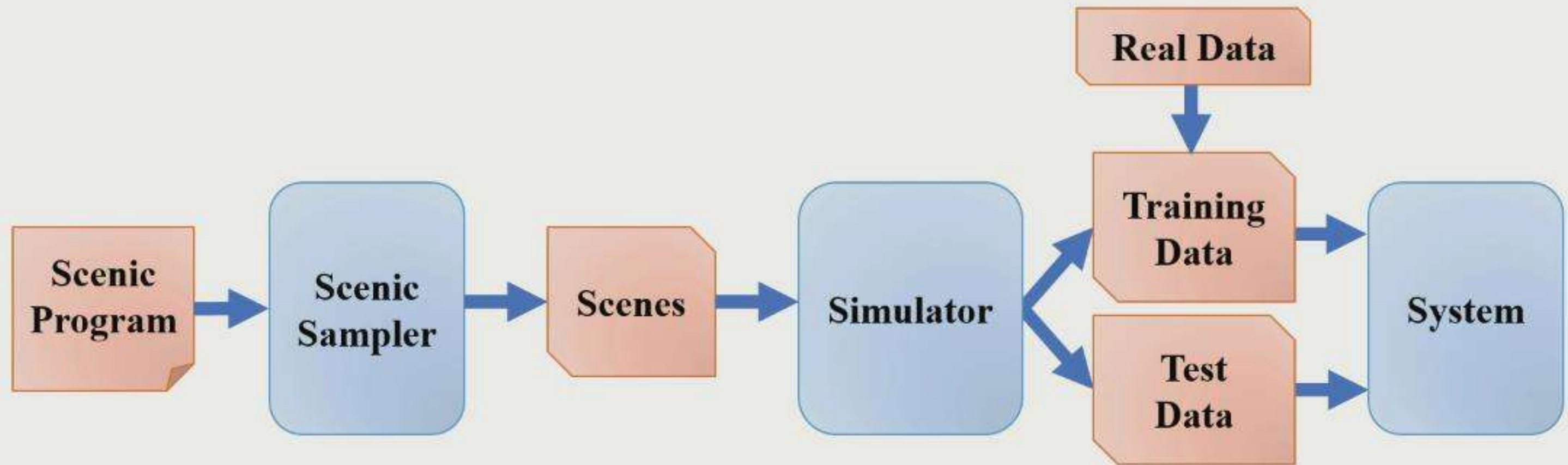


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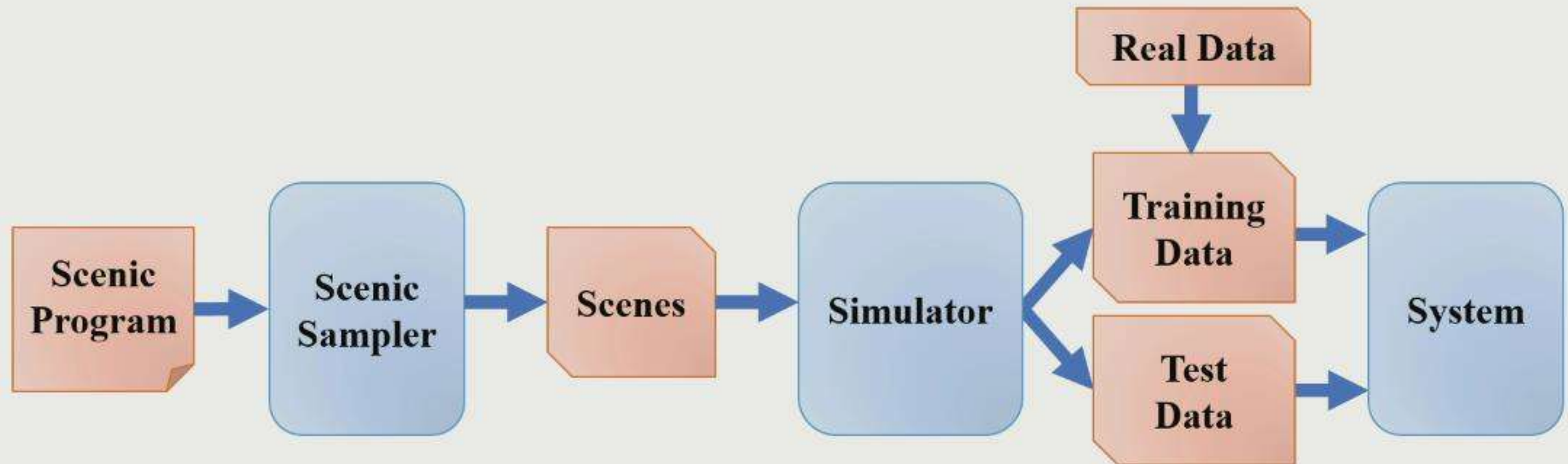
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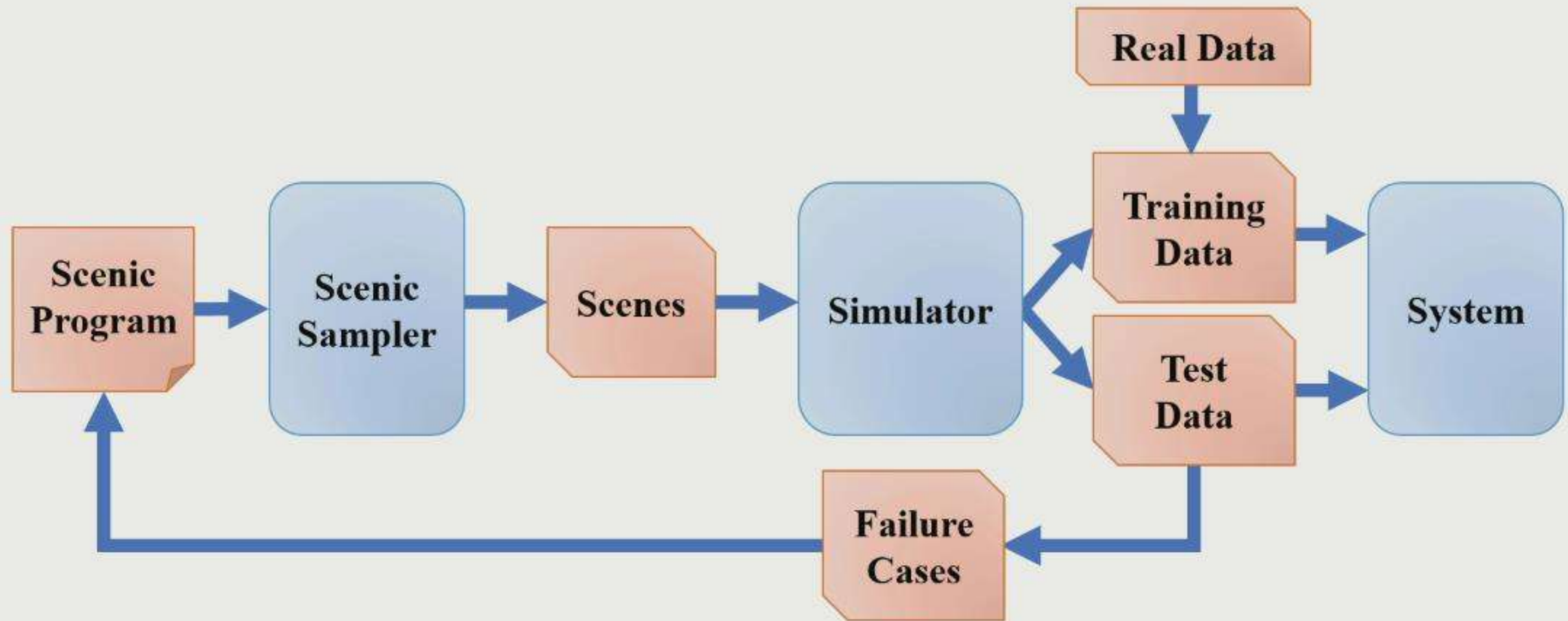


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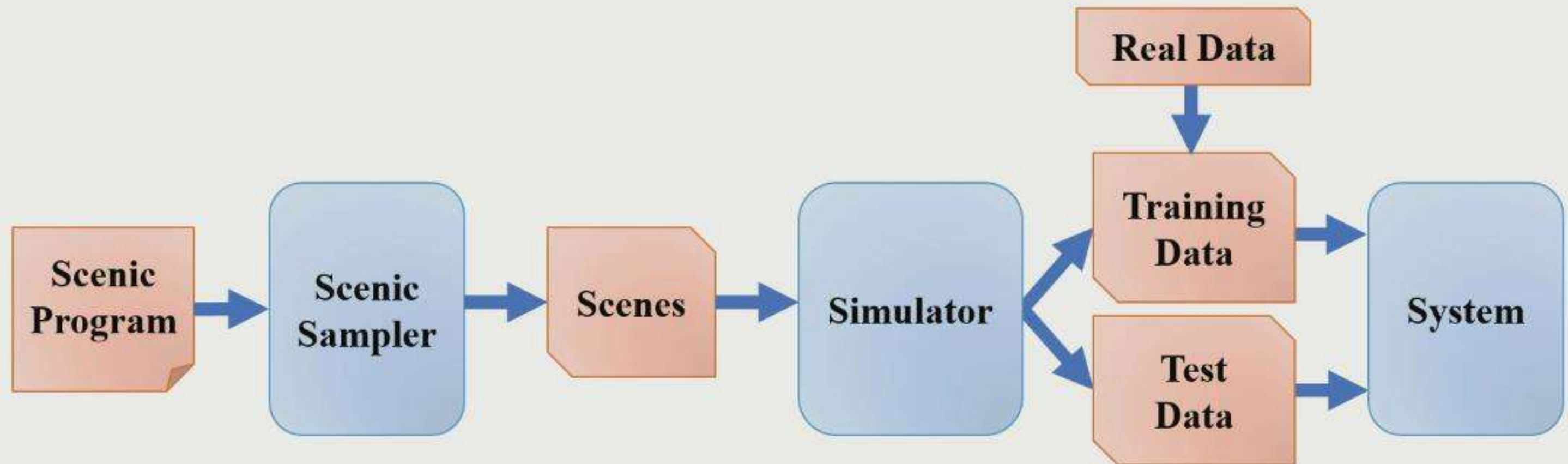




# Related Work: PPLs

- [1] Gordon et al., *FOSE 2014*.
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# Related Work: PPLs

- SCENIC's semantics is that of a standard imperative PPL (e.g. [1])
- PPLs have been used as generative models of graphics
  - e.g. Quicksand [2], Picture [3]

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- PPLs have been used as generative models of graphics
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- The main differences in SCENIC:
  - emphasis on generation, not inference
  - domain-specificity

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# Related Work: Graphics & ML

- [4] Fisher et al., *SIGGRAPH* 2012.
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- Scene synthesis from examples or grammars [4, 5]
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# Related Work: Graphics & ML

- Scene synthesis from examples or grammars [4, 5]
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- The main differences in SCENIC:
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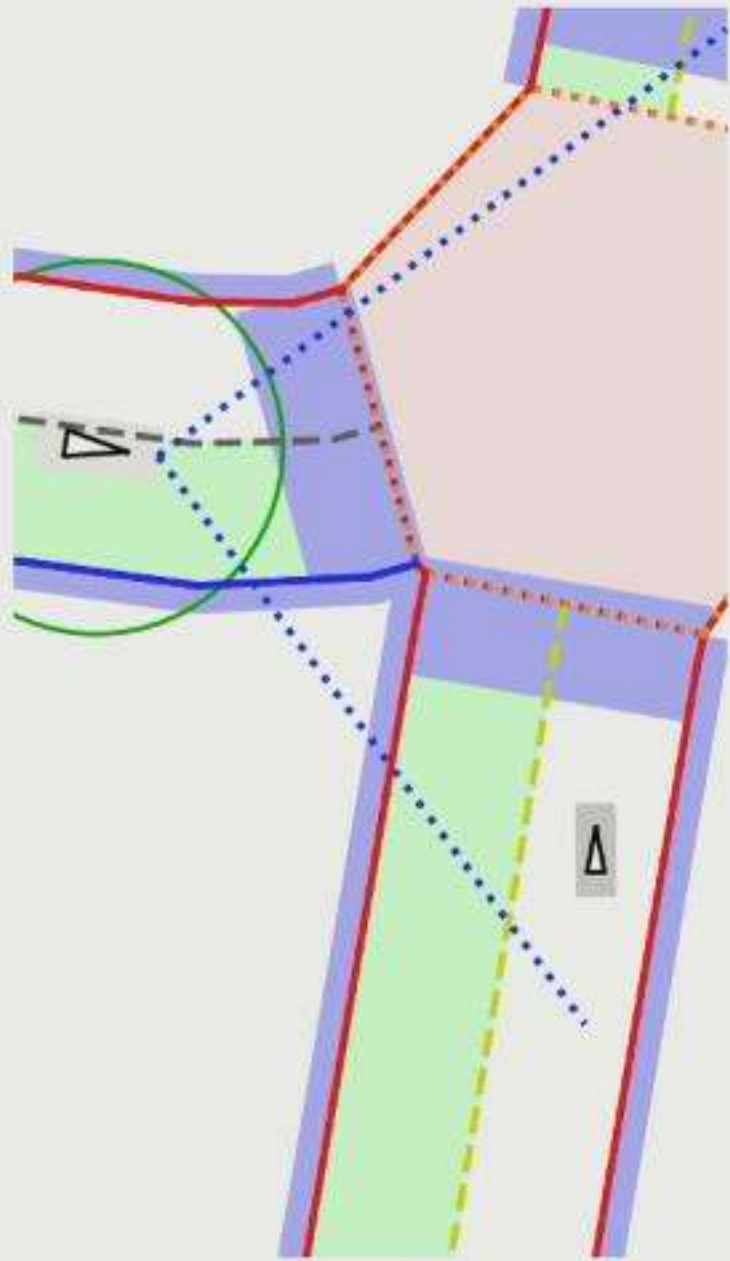
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# Example: a Badly-Parked Car



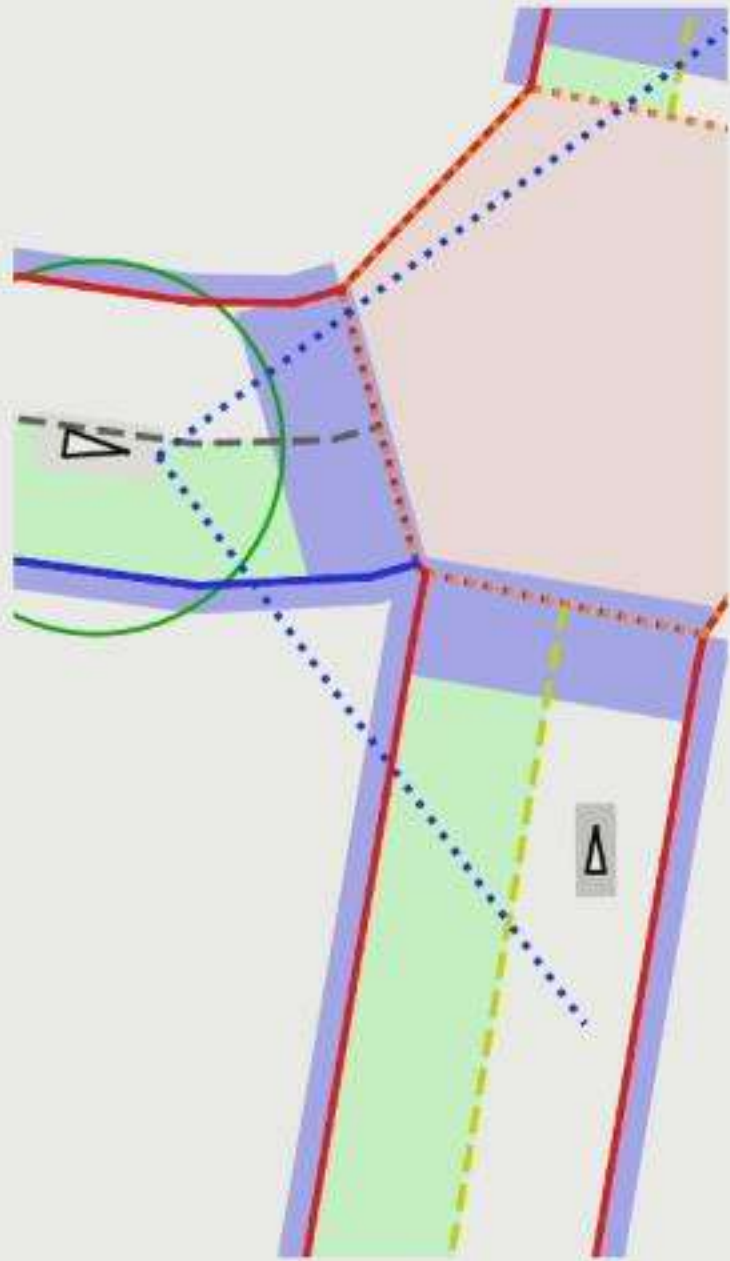


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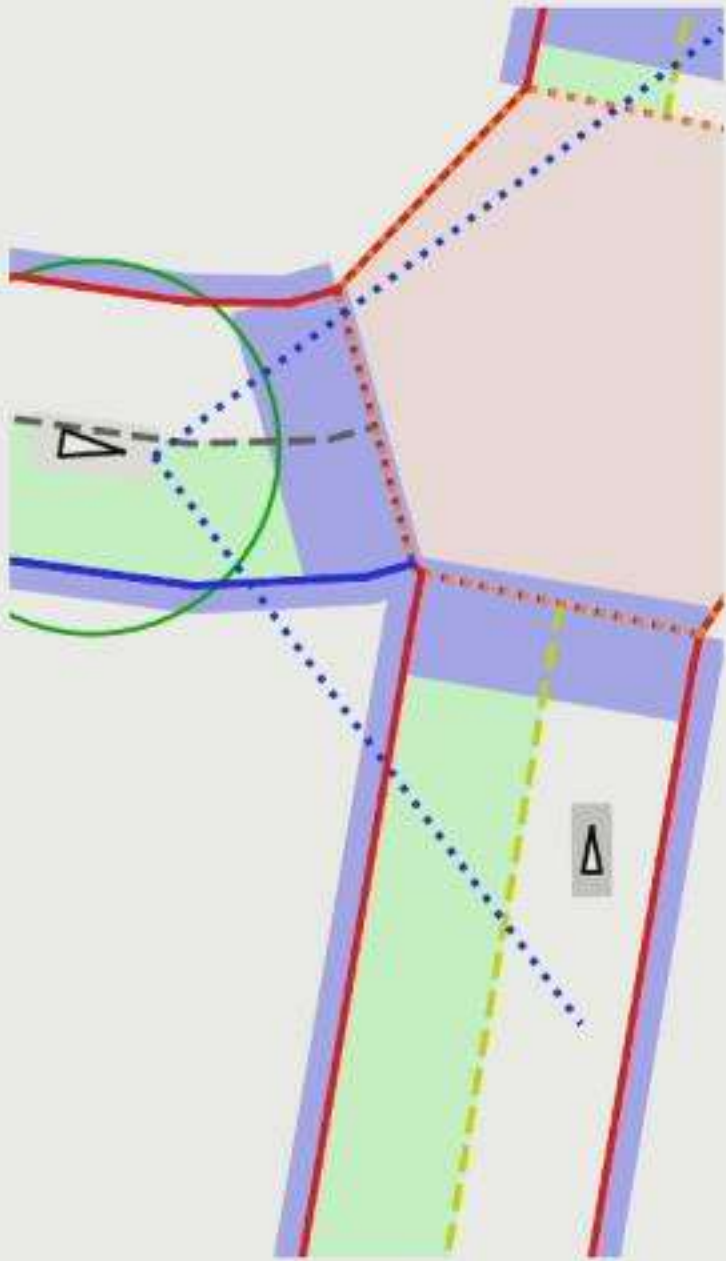


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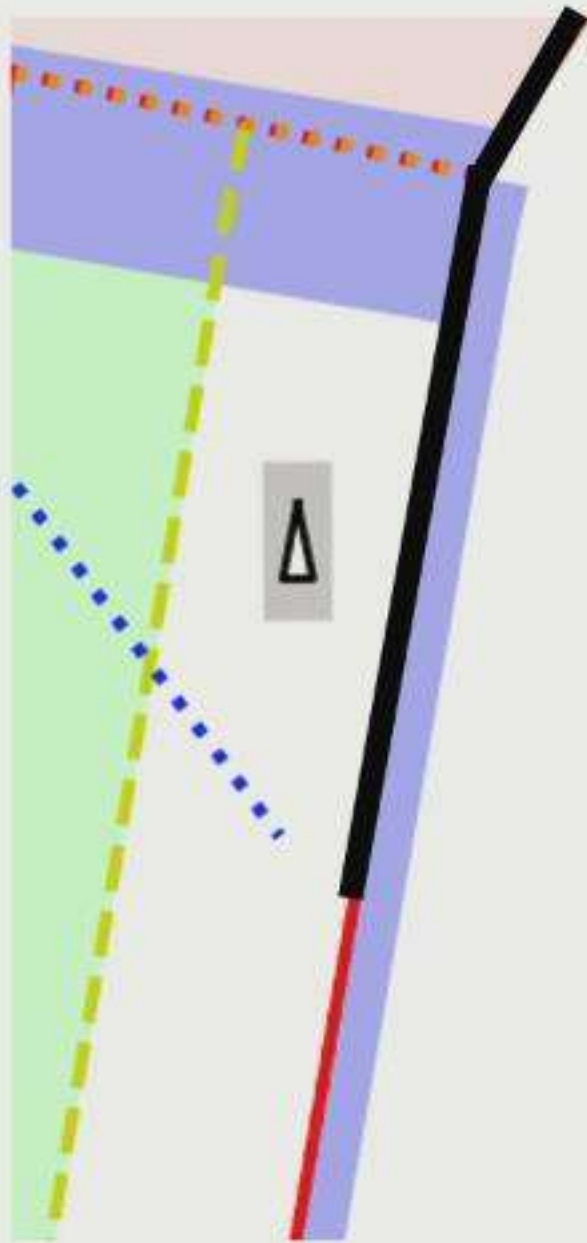
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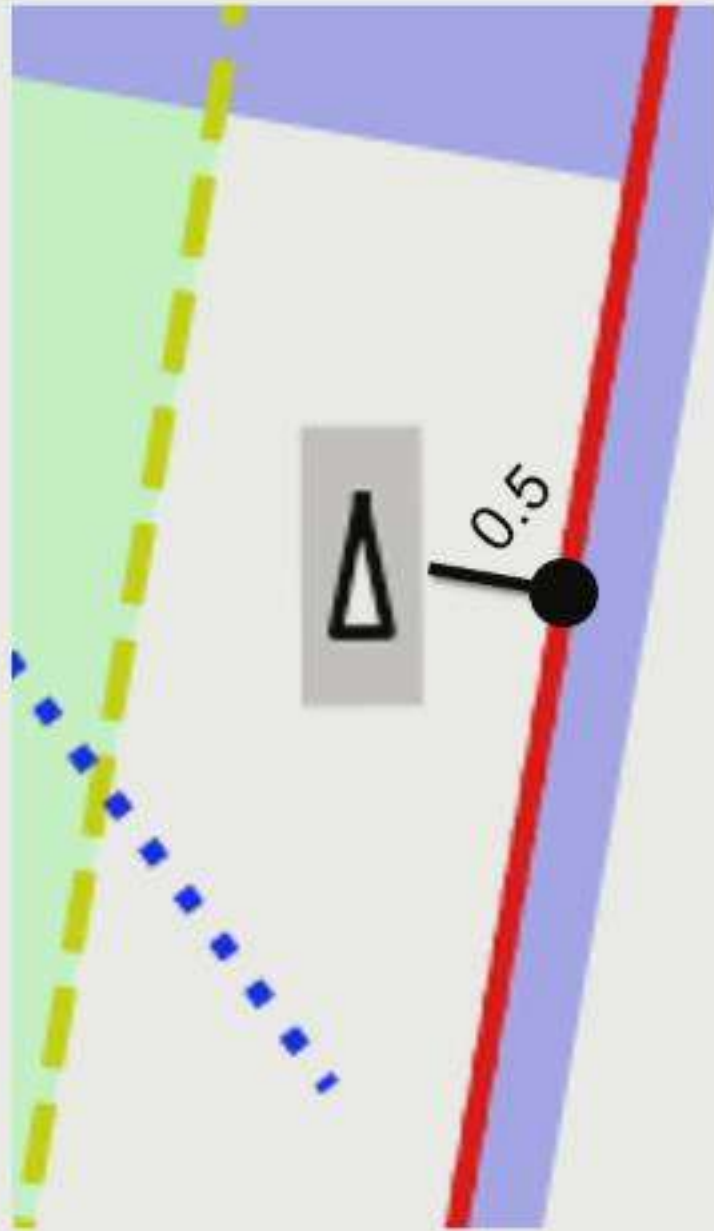
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Car left of (spot offset by -0.5 @ 0),
    facing badAngle relative to roadDirection
```

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# Specifiers

- Syntactic elements defining properties of an object
  - Can be combined in arbitrary ways to build up a complete definition

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Specifies  
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- SCENIC has 9 completely different *position* specifiers
  - All mirroring ways we use natural language to talk about positions



# Specifiers Capture Dependencies

- Can depend on other properties and other specifiers

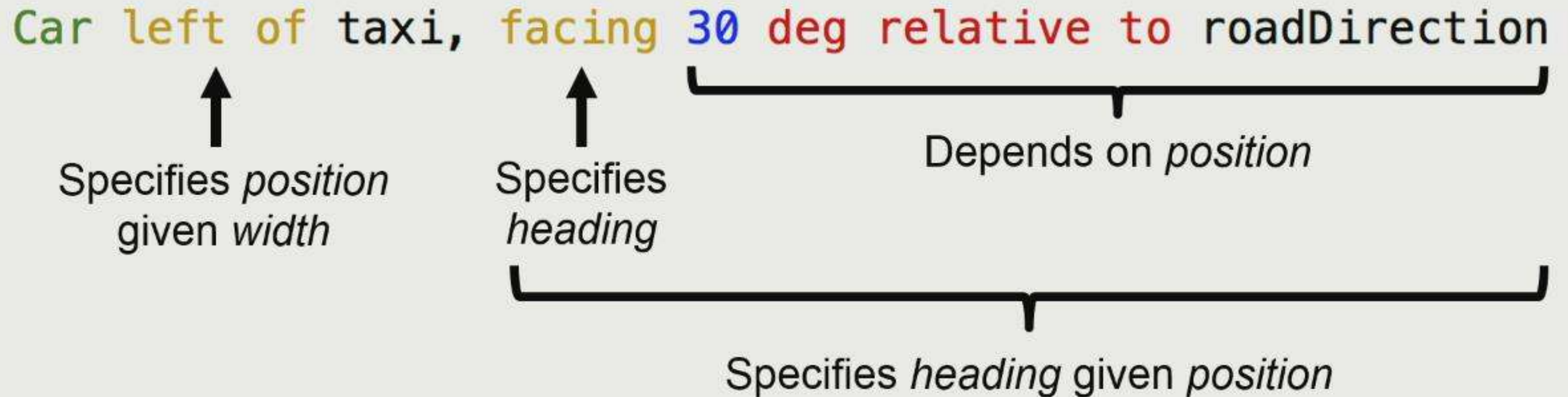
Car left of taxi, facing 30 deg relative to roadDirection



Specifies *position*  
given *width*

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# Domain-Specific Sampling Techniques

- Prune infeasible parts of the space by dilating polygons

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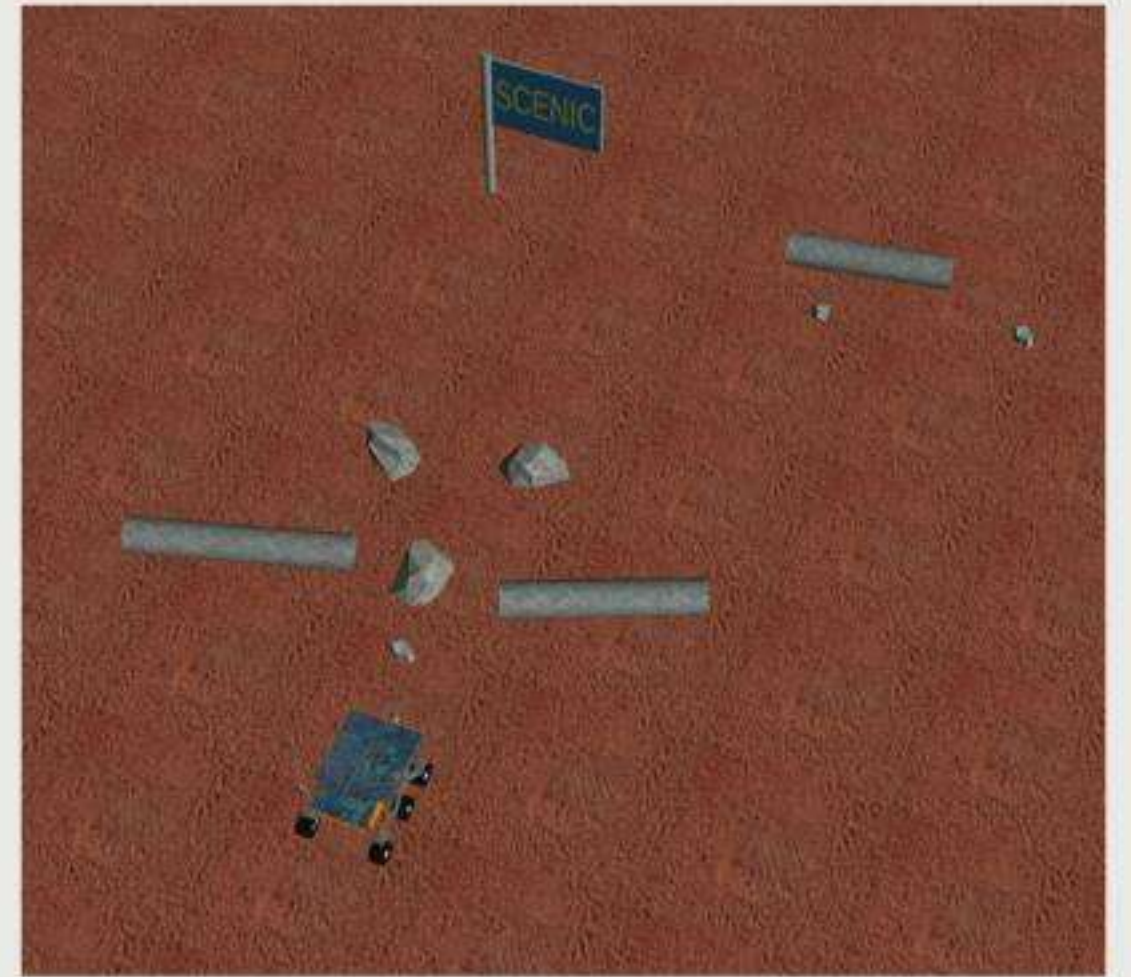
require distance to taxi  $\leq 5$   
require  $15 \text{ deg} \leq (\text{relative heading of taxi}) \leq 45 \text{ deg}$





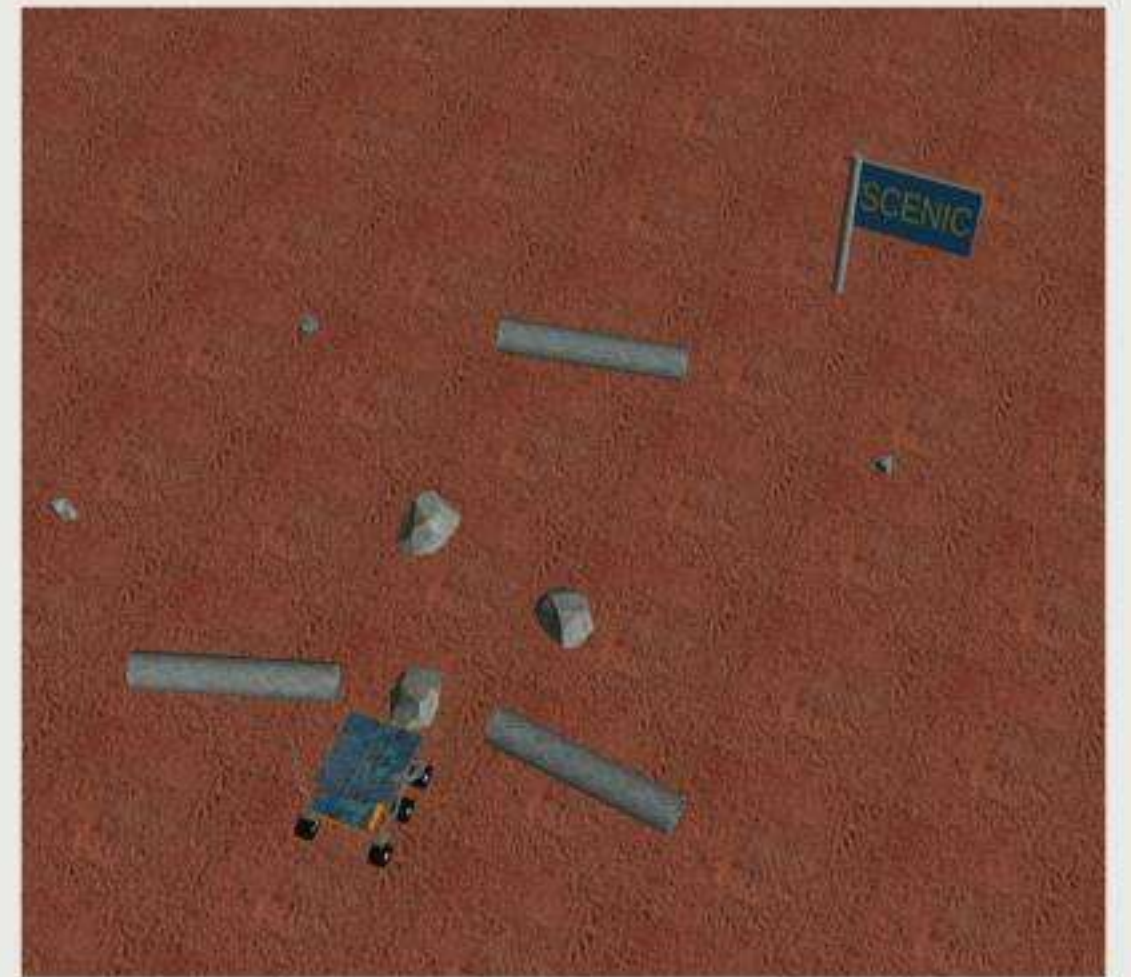
# Applications of Scenic

- Exploring system performance
  - Generating specialized test sets



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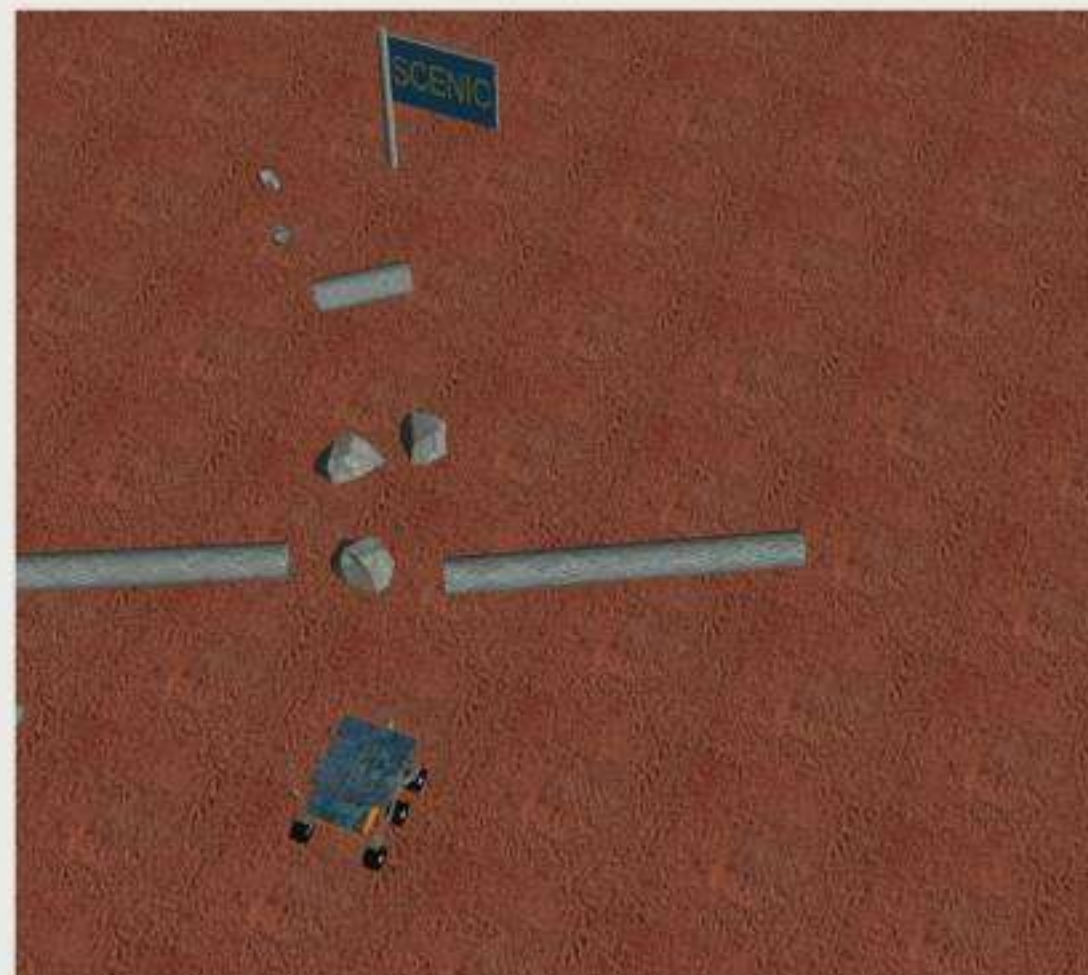
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- Debugging a known failure
  - Generalizing in different directions





# Applications of Scenic

- Exploring system performance
  - Generating specialized test sets
- Debugging a known failure
  - Generalizing in different directions
- Designing more effective training sets
  - Training on hard cases



# Outline

1. Control Improvisation
  - Definition and motivating applications
2. Theory of CI
  - Efficient algorithms and hardness results
3. Designing and Analyzing Perception Systems
4. **Conclusion and Future Work**

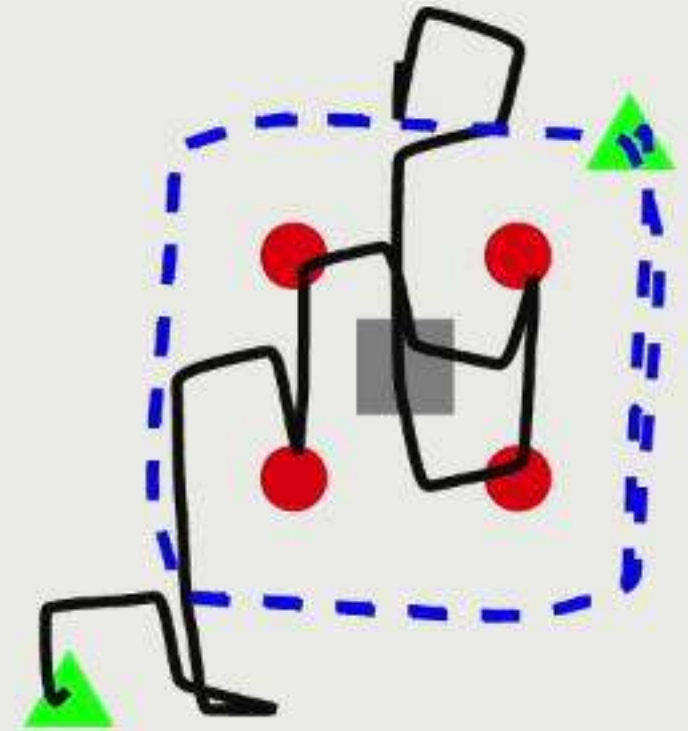


# Summary and Conclusions

- Algorithmic Improvisation: a framework for randomized synthesis
  - Data generation, planning, fuzz testing, music improvisation, human modeling...

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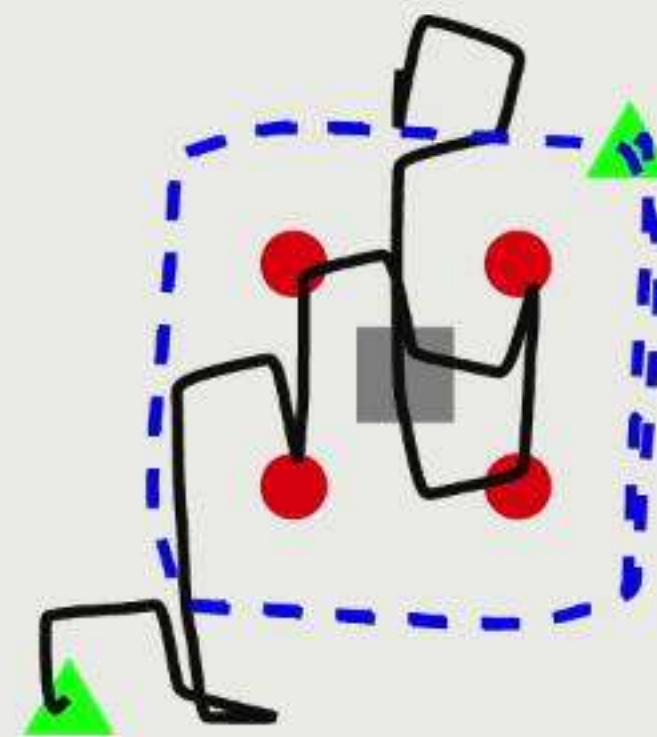
- Algorithmic Improvisation: a framework for randomized synthesis
  - Data generation, planning, fuzz testing, music improvisation, human modeling...
- Applications to safe autonomy
  - Controller synthesis, synthetic data generation





# Summary and Conclusions

- Algorithmic Improvisation: a framework for randomized synthesis
  - Data generation, planning, fuzz testing, music improvisation, human modeling...
- Applications to safe autonomy
  - Controller synthesis, synthetic data generation
- Randomized formal methods can contribute in many ways to the design and verification of autonomous systems



# The Future of Algorithmic Improvisation

- Fundamentally new problem in CS → rich possibilities at all levels



# The Future of Algorithmic Improvisation

- Fundamentally new problem in CS → rich possibilities at all levels
- Intelligent data generation for a variety of data types
- Environment modeling, including modeling dynamic agents
- Generalized theory of CI enabling new applications

# The Future of Algorithmic Improvisation

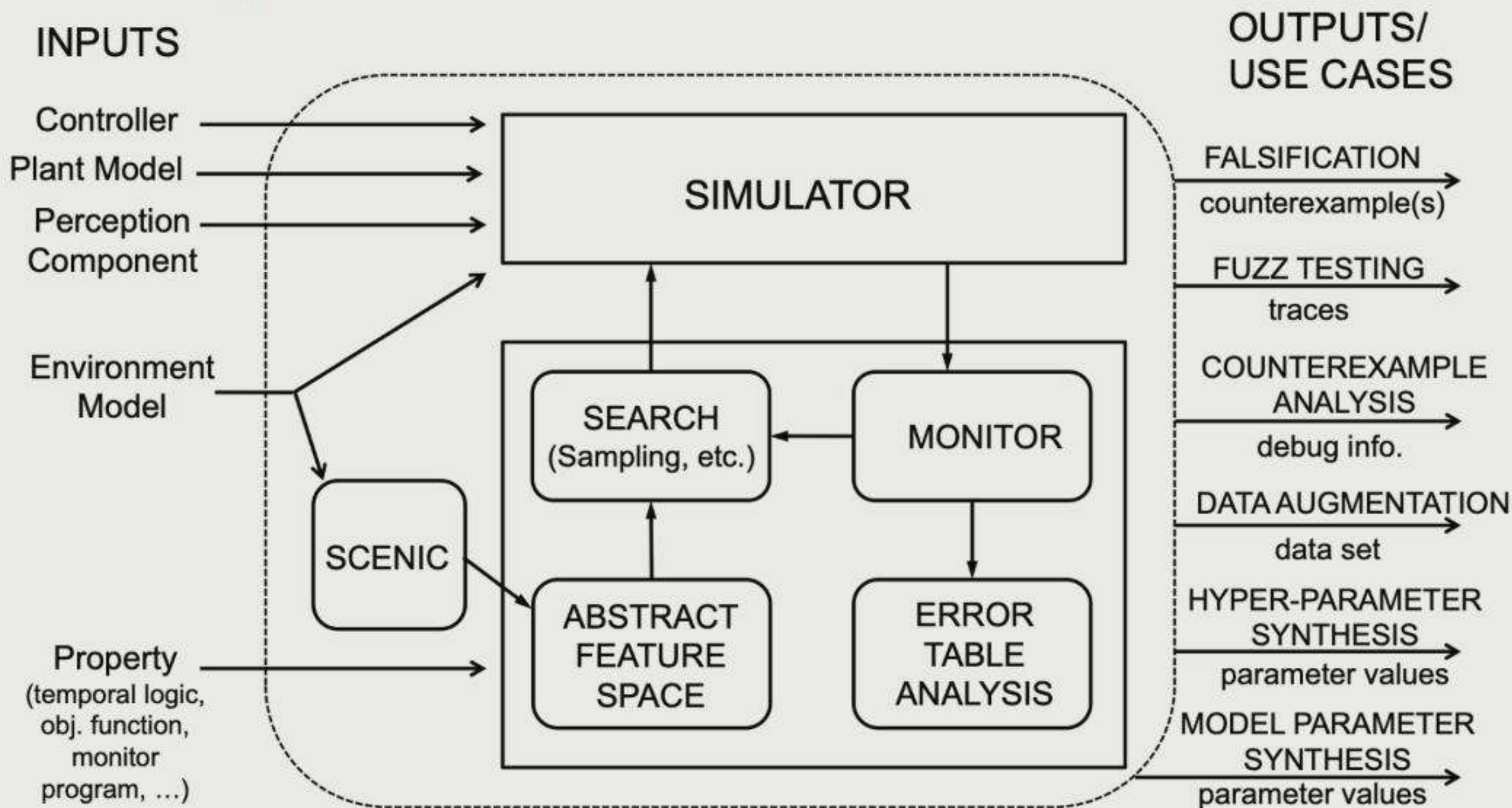
- Fundamentally new problem in CS → rich possibilities at all levels
- Intelligent data generation for a variety of data types
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- Generalized theory of CI enabling new applications
- Verifying ML/AI-based systems: the VerifAI toolkit [CAV 2019]



# VERIFAI: A Toolkit for the Design and Analysis of

[CAV'19]

# AI-Based Systems <https://github.com/BerkeleyLearnVerify/VerifAI>





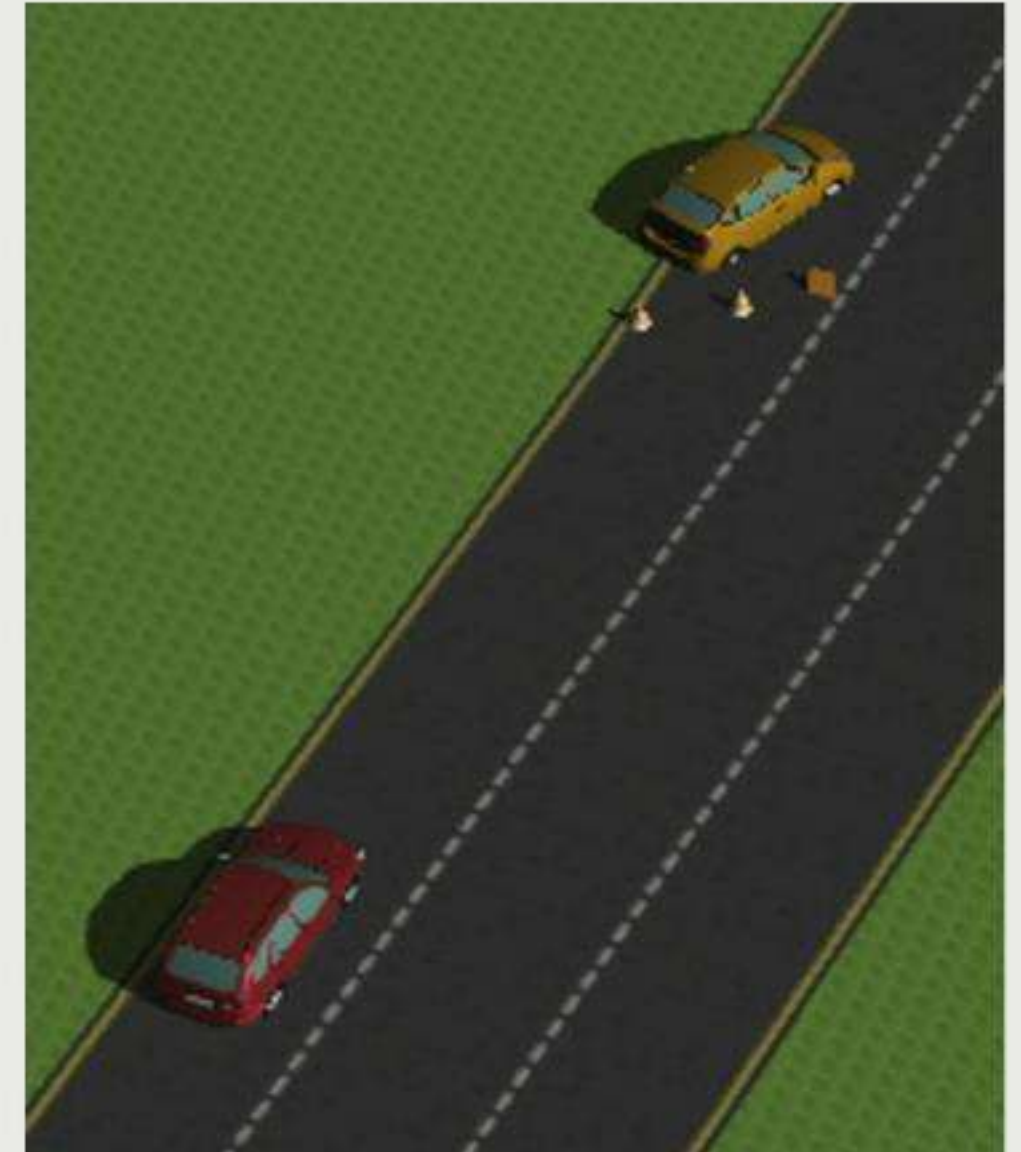
# Modeling Case Study in the SCENIC Language

```
# Pick location for blockage randomly along curb
blockageSite = OrientedPoint on curb

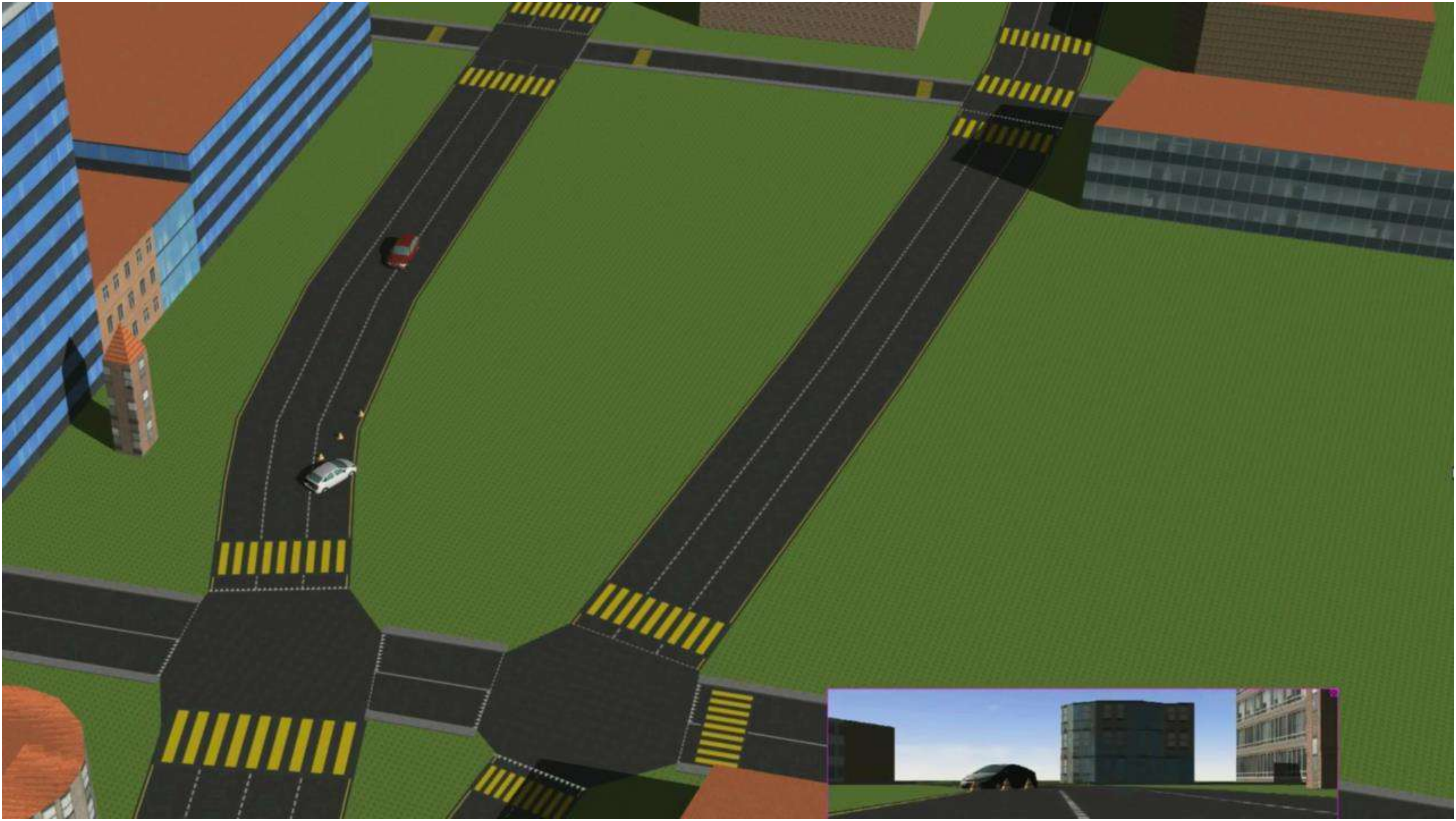
# Place traffic cones
spot1 = OrientedPoint left of blockageSite by (0.3, 1)
cone1 = TrafficCone at spot1,
        facing (0, 360) deg

...

# Place disabled car ahead of cones
SmallCar ahead of spot2 by (-1, 0.5) @ (4, 10),
        facing (0, 360) deg
```









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*Thank you!*